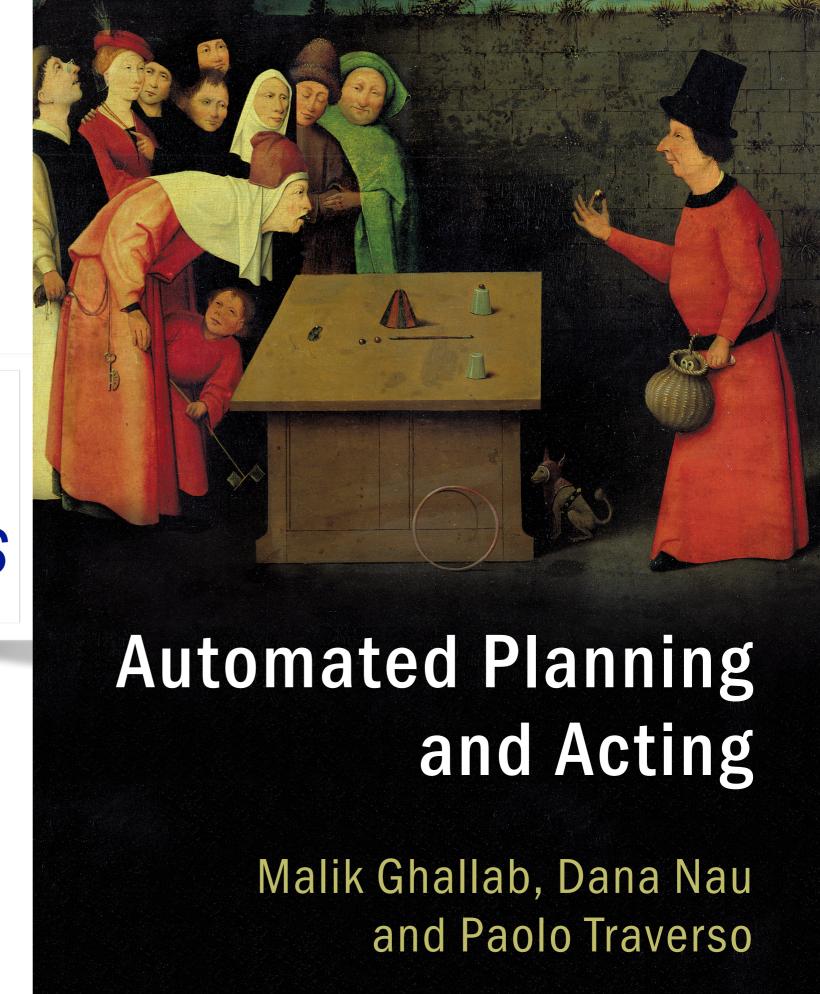
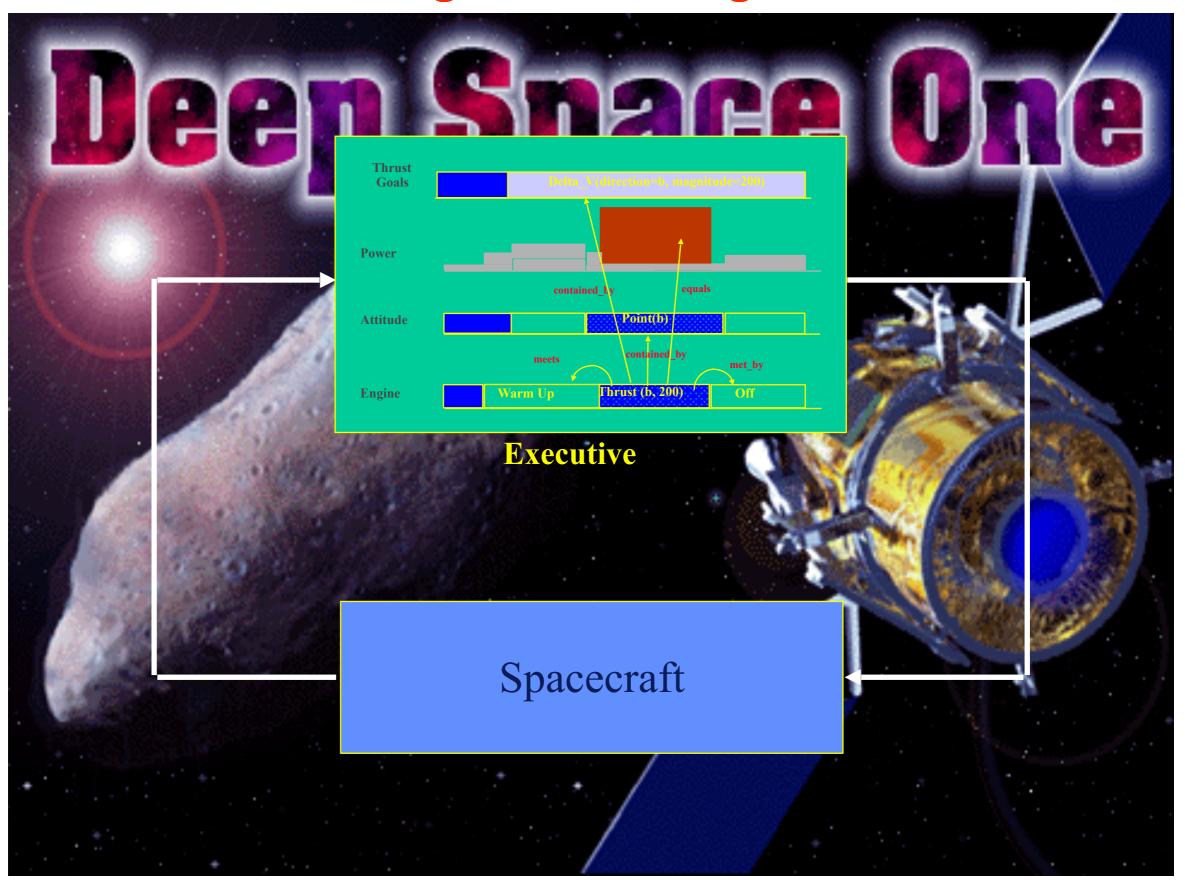
Deliberation with Temporal Models



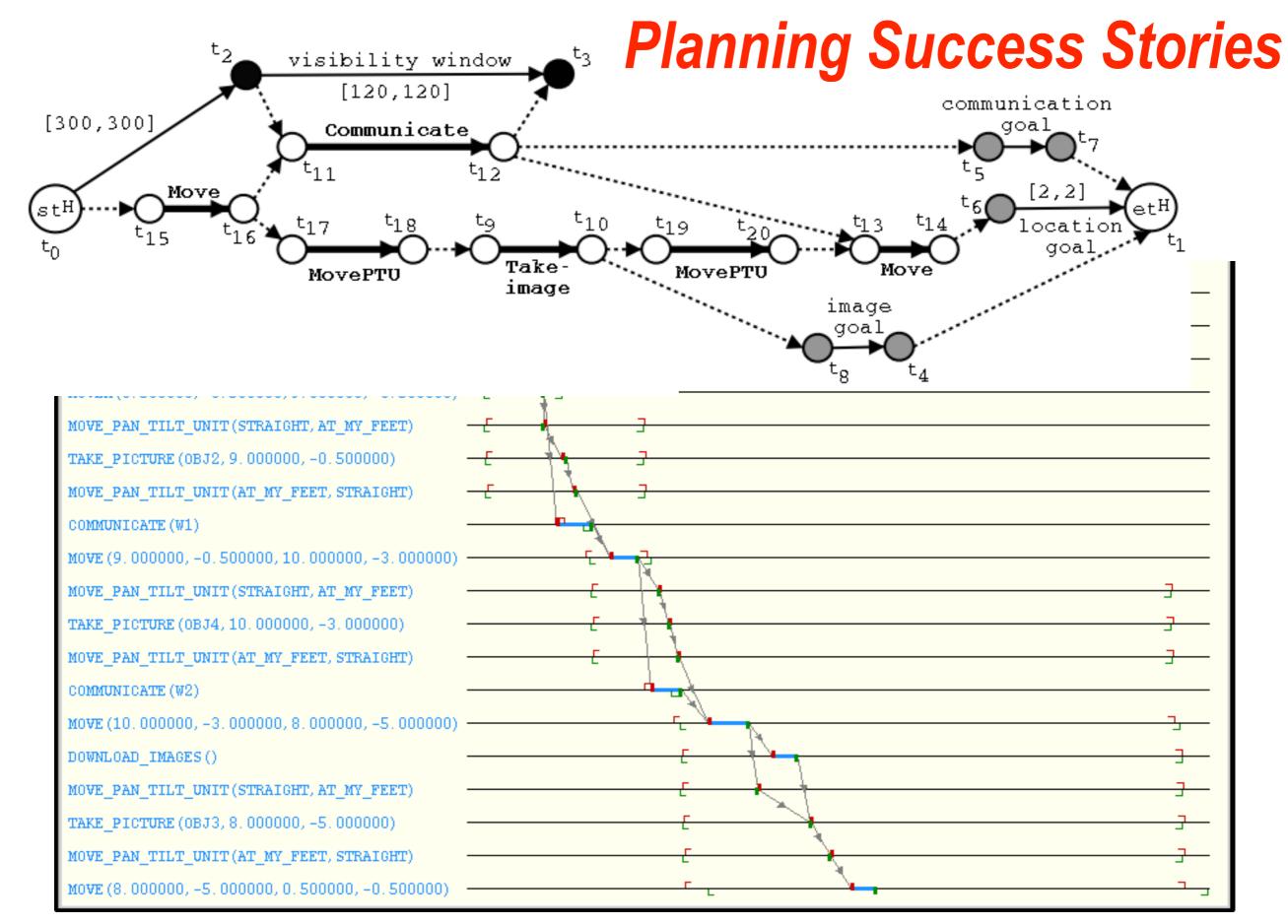
Planning and Acting Success Stories



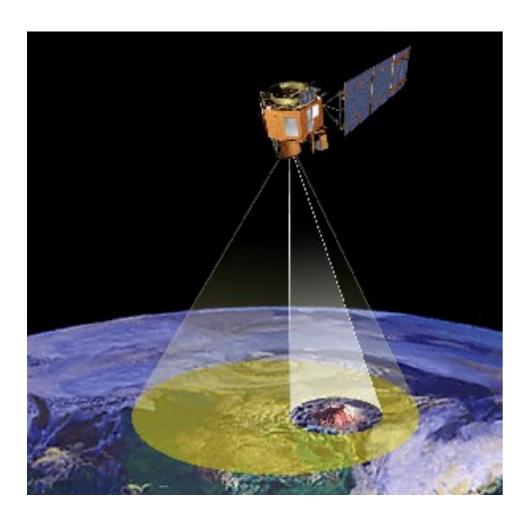
Planning Success Stories



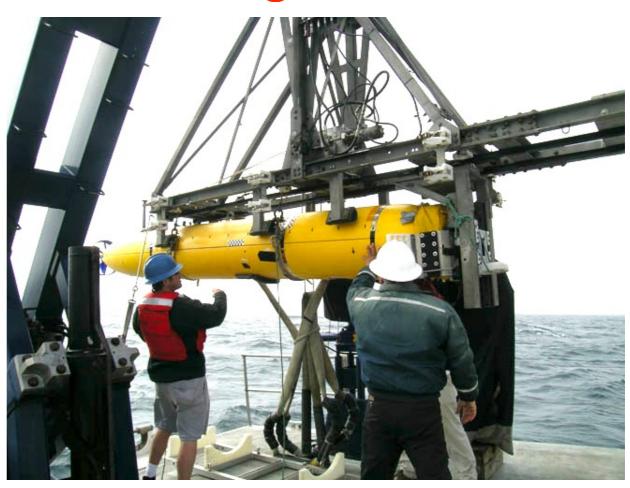
[IxTeT, LAAS]



Planning Success Stories







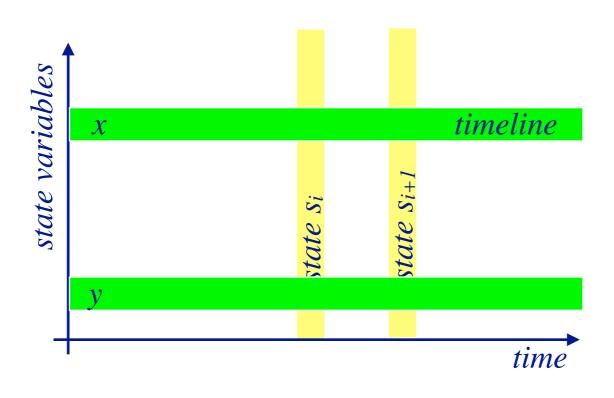
[T-ReX, MBARI]

Common point to these success stories: explicit representation of time

Motivations for Temporal Models

- Duration of actions
- Delayed effects, conditions, and resources borrowed or consumed at various moments along an action duration
- Timed goals with relative or absolute temporal constraints
- Exogenous events expected to occur in the future time
- Maintenance actions: maintain a property (≠ changing a value),
 e.g., tracking a moving target, keeping a spring latch in position
- Concurrency of actions with interacting and joint effects
- Delayed commitment: instantiation at acting time

Temporal Models



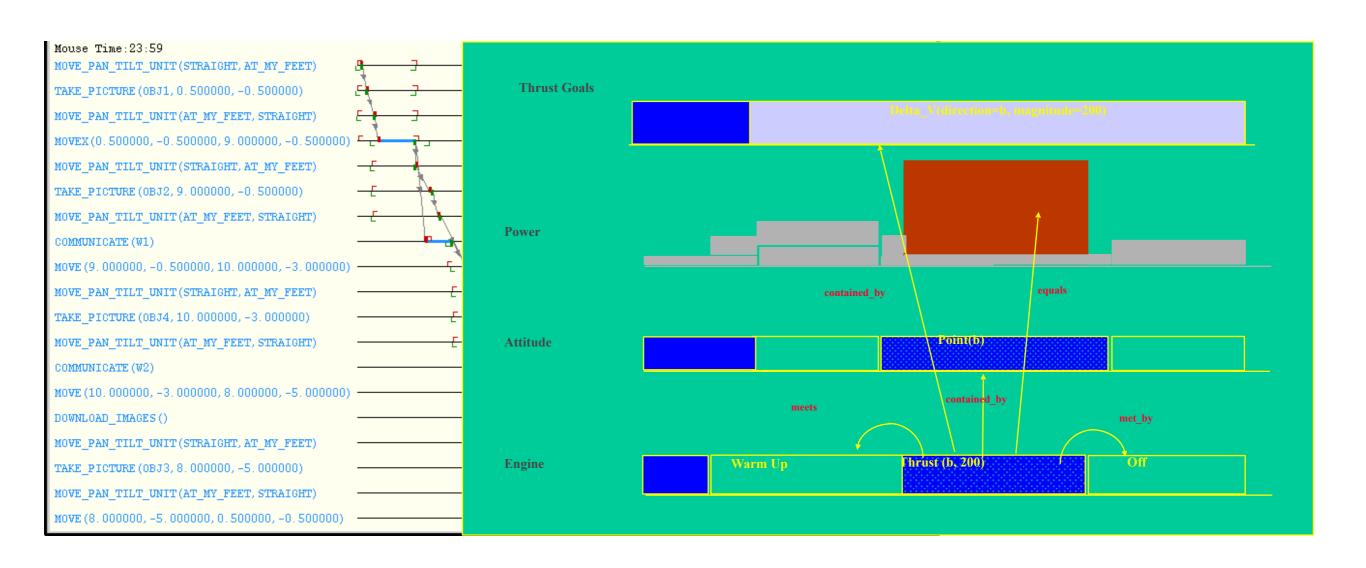
Motivations for Temporal Models

	States	Timelines
Duration of actions	√	V
Delayed effects	√	√
Timed goals	√	√
Exogenous events	~	√
Maintenance actions	√	\checkmark
Concurrency	_	V
Delayed commitment	_	√

Timeline

Timeline

- A set of constraints on state variables and events
- Reflects *predicted* actions and events
- Timeline planning akin to constraint-based planning



Outline

- ✓ Introduction
- Representation
 - Timelines
 - Actions and tasks
 - Chronicles
- Temporal planning
- Consistency and controllability
- Acting with executable primitives
- Acting with atemporal refinement
- Conclusion

Representation

- Quantitative discrete model of time
 - variables referring to time points
 - simple constraints

$$d \le t' - t \le d'$$

- Temporal assertions
 - persistance over an interval
 - change over an interval

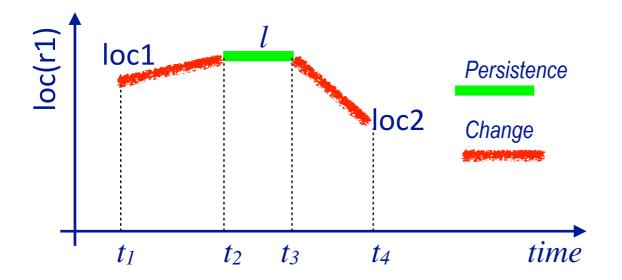
$$[t_1, t_2]x = v$$

$$[t_1, t_2]x:(v_1, v_2)$$

Timeline

Partially predicted evolution of a state variable: a pair (T,C)

- T: temporal assertions
- C: contraints



$$[t_1, t_2] loc(r1) : (loc1, l)$$

 $[t_2, t_3] loc(r1) = l$
 $[t_3, t_4] loc(r1) : (l, loc2)$
 $t_1 < t_2 < t_3 < t_4$
 $l \neq loc1$
 $l \neq loc2$

To restrict the value of loc(r1) in $[t_1, t_2]$

$$[t_1, t_1 + 1]$$
 loc(r1):(loc1,route)
 $[t_2 - 1, t_2]$ loc(r1):(route, l)
 $[t_1 + 1, t_2 - 1]$ loc(r1)= route

Consistent and Secure Timeline

- ▶ A ground instance of (*T*,*C*) is consistent if it satisfies *C* and no state variable in *T* has more than on value at the same time
- ▶ (*T*,*C*) is *consistent* if it has a consistent ground instance
- ▶ (T,C) is secure if it is consistent and
 every ground instance that satisfies C is consistent

```
[t_1,t_2] 	ext{loc}(r) = 	ext{loc}1 \ [t_2,t_3] 	ext{loc}(r): (	ext{loc}1,	ext{loc}2)  secure timeline t_1 < t_2 < t_3
```

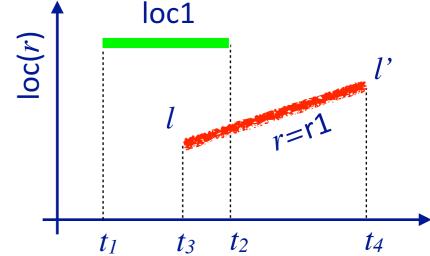
Consistent and Secure Timeline

- ▶ A ground instance of (*T*,*C*) is consistent if it satisfies *C* and no state variable in *T* has more than on value at the same time
- ▶ (*T*,*C*) is *consistent* if it has a consistent ground instance
- ▶ (T,C) is secure if it is consistent and
 every ground instance that satisfies C is consistent

$$[t_1, t_2] loc(r) = loc1$$

 $[t_3, t_4] loc(r1) : (l, l')$
 $t_1 < t_2, t_3 < t_4$

timeline consistent but not secure



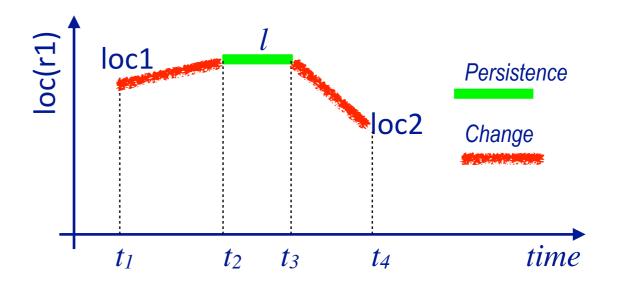
Conflicting assertions

=> separation constraints

$$r
eq r1$$
 $t_2 < t_3$
 $t_4 < t_1$
 $t_2 = t_3, r = r1, l = loc1$
 $t_4 = t_1, r = r1, l' = loc1$

Causally supported timeline

- Causal support of the value of x: reasons that substantiate it
 - Prior knowledge about current state or dynamics of environment
 - Observation
 - Prediction of actions effects



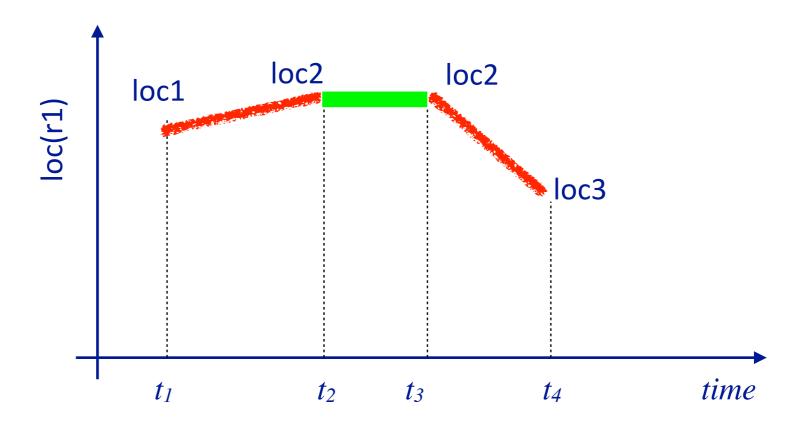
Causally supported timeline:
 all its assertions have a causal support

Finding causal support

Adding a persistence assertion

$$[t_1, t_2]$$
loc(r1):(loc1,loc2), $[t_3, t_4]$ loc(r1):(loc2,loc3) $t_1 < t_2 < t_3 < t_4$

$$[t_2, t_3] \log(r1) = \log 2$$

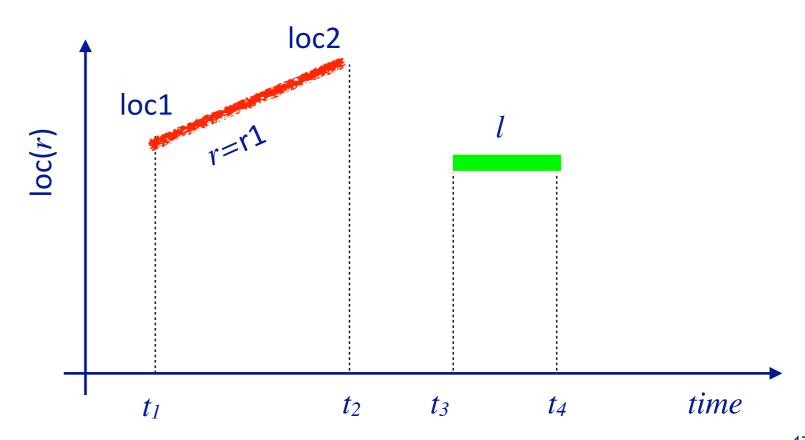


Finding causal support

- Adding a persistence assertion
- Adding constraints

$$[t_1, t_2]$$
loc(r1):(loc1,loc2), $[t_3, t_4]$ loc(r) = l
 $t_1 < t_2 < t_3 < t_4$

$$t_2 = t_3, r = r1, l = loc2$$

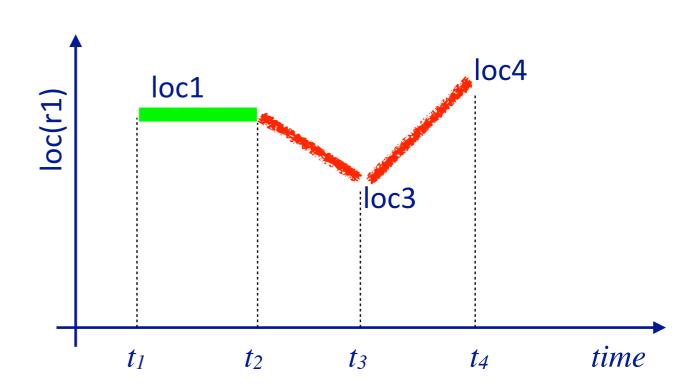


Finding causal support

- Adding a persistence assertion
- Adding constraints
- ▶ Adding a change assertion → corresponds to an additional action

$$[t_1, t_2]$$
loc(r1)= loc1, $[t_3, t_4]$ loc(r1):(loc3,loc4) $t_1 < t_2 < t_3 < t_4$

$$[t_2, t_3] loc(r1):(loc1, loc3)$$



Example

Domain objects

$$r \in Robots, k \in Cranes, c \in Containers$$

 $p \in Piles, d \in Docks, w \in Waypoints$

State variables

$$\begin{aligned} & \mathsf{loc}(r) \in \mathit{Docks} \cup \mathit{Waypoints} & \mathsf{for}\ r \in \mathit{Robots} \\ & \mathsf{freight}(r) \in \mathit{Containers} \cup \{\mathsf{empty}\} & \mathsf{for}\ r \in \mathit{Robots} \\ & \mathsf{grip}(k) \in \mathit{Containers} \cup \{\mathsf{empty}\} & \mathsf{for}\ k \in \mathit{Cranes} \\ & \mathsf{pos}(c) \in \mathit{Robots} \cup \mathit{Cranes} \cup \mathit{Piles} & \mathsf{for}\ c \in \mathit{Containers} \\ & \mathsf{stacked-on}(c) \in \mathit{Containers} \cup \{\mathsf{empty}\} & \mathsf{for}\ c \in \mathit{Containers} \\ & \mathsf{top}(p) \in \mathit{Containers} \cup \{\mathsf{empty}\} & \mathsf{for}\ p \in \mathit{Piles} \\ & \mathsf{occupant}(d) \in \mathit{Robots} \cup \{\mathsf{empty}\} & \mathsf{for}\ d \in \mathit{Docks} \end{aligned}$$

Rigid relations

attached
$$\subseteq (Cranes \cup Piles) \times Docks$$

adjacent $\subseteq Docks \times Waypoints$
connected \subseteq Waypoints \times Waypoints

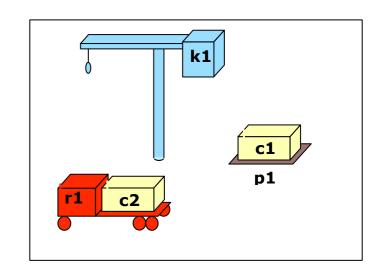
Example

Primitive actions

```
\begin{aligned} &\mathsf{leave}(r,d,w) : \mathsf{robot}\ r\ \mathsf{leaves}\ \mathsf{dock}\ d\ \mathsf{to}\ \mathsf{an}\ \mathsf{adjacent}\ \mathsf{waypoint}\ w\\ &\mathsf{enter}(r,d,w) : r\ \mathsf{enters}\ d\ \mathsf{from}\ \mathsf{an}\ \mathsf{adjacent}\ \mathsf{waypoint}\ w\\ &\mathsf{navigate}(r,w,w') : r\ \mathsf{navigates}\ \mathsf{from}\ \mathsf{waypoint}\ w\ \mathsf{to}\ \mathsf{a}\ \mathsf{connected}\ \mathsf{one}\ w'\\ &\mathsf{stack}(k,c,p) : \mathsf{crane}\ k\ \mathsf{holding}\ \mathsf{container}\ c\ \mathsf{stacks}\ \mathsf{it}\ \mathsf{on}\ \mathsf{top}\ \mathsf{of}\ \mathsf{pile}\ p\\ &\mathsf{put}(k,c,r) : \mathsf{crane}\ k\ \mathsf{holding}\ \mathsf{a}\ \mathsf{container}\ c\ \mathsf{from}\ \mathsf{the}\ \mathsf{top}\ \mathsf{of}\ \mathsf{pile}\ p\\ &\mathsf{take}(k,c,r) : \mathsf{crane}\ k\ \mathsf{takes}\ \mathsf{container}\ c\ \mathsf{from}\ \mathsf{robot}\ r\end{aligned}
```

Primitives

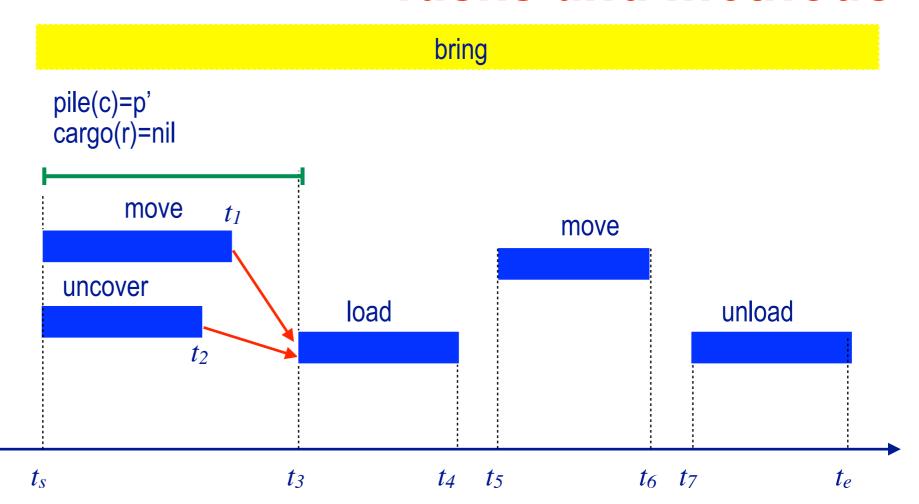
```
take(k, c, r) assertions: [t_s, t_e] \mathsf{pos}(c) : (r, k) [t_s, t_e] \mathsf{grip}(k) : (\mathsf{empty}, c) [t_s, t_e] \mathsf{freight}(r) : (c, \mathsf{empty}) [t_s, t_e] \mathsf{loc}(r) = d constraints: \mathsf{attached}(k, d)
```



```
leave(r,d,w) assertions: [t_s,t_e] loc(r):(d,w) [t_s,t_e] occupant(d):(r,empty) constraints: t_e \leq t_s + \delta_1 adjacent(d,w)
```

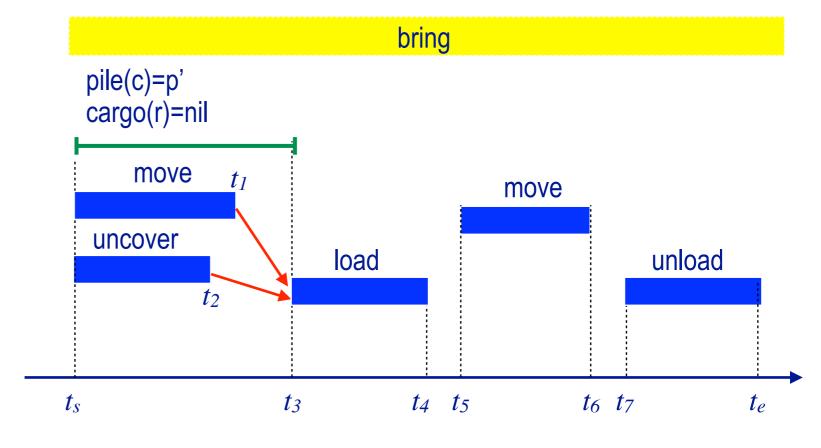
Tasks

 $[t_s, t_e]$ bring(r, c, p)



$$egin{aligned} [t_s,t_1] \mathsf{move}(r,d) \ [t_s,t_2] \mathsf{uncover}(k,c,p) \ [t_3,t_4] \mathsf{load}(k,r,c,p) \ [t_7,t_e] \mathsf{unload}(k,r,c,p) \end{aligned}$$

Methods



 $\mathsf{m\text{-}bring}(r,c,p,p',d,d',k,k')$

task: bring(r, c, p)

refinement: $[t_s, t_1]$ move(r, d')

 $[t_s, t_2]$ uncover(c, p')

 $[t_3,t_4]$ load(k',r,c,p')

 $[t_5, t_6]$ move(r, d)

 $[t_7, t_e]$ unload(k, r, c, p)

assertions: $[t_s, t_3]$ pile(c) = p'

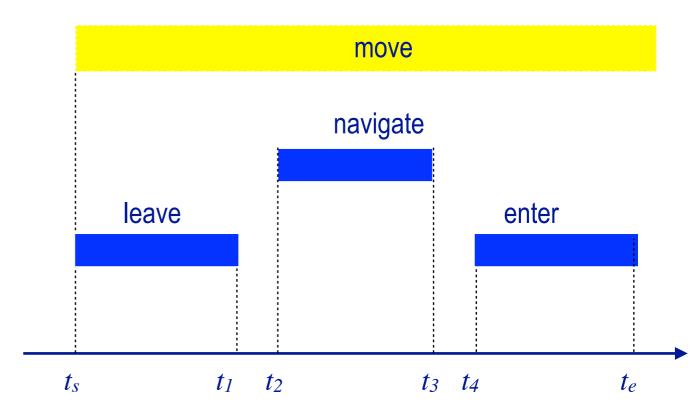
 $[t_s, t_3]$ freight (r) = empty

constraints: attached(p', d'), attached(p, d), $d \neq d'$

 $\mathsf{attached}(k',d')$, $\mathsf{attached}(k,d)$

 $t_1 \le t_3, \ t_2 \le t_3, \ t_4 \le t_5, \ t_6 \le t_7$

Methods



```
\mathsf{m}	ext{-}\mathsf{move1}(r,d,d',w,w')
```

task: move(r, d)

refinement: $[t_s, t_1]$ leave(r, d', w')

 $[t_2, t_3]$ navigate(w', w)

 $[t_4, t_e]$ enter(r, d, w)

assertions: $[t_s, t_s + 1] loc(r) = d'$

constraints: adjacent(d, w), adjacent(d', w'), $d \neq d'$

connected(w, w')

$$t_1 \le t_2, \ t_3 \le t_4$$

Methods

 $\mathsf{m} ext{-}\mathsf{uncover}(c,p,k,d,p')$

task: uncover(c, p)

refinement: $[t_s, t_1]$ unstack(k, c', p)

 $[t_2, t_3]$ stack(k, c', p')

 $[t_4, t_e]$ uncover(c, p)

assertions: $[t_s, t_s + 1]$ pile(c) = p

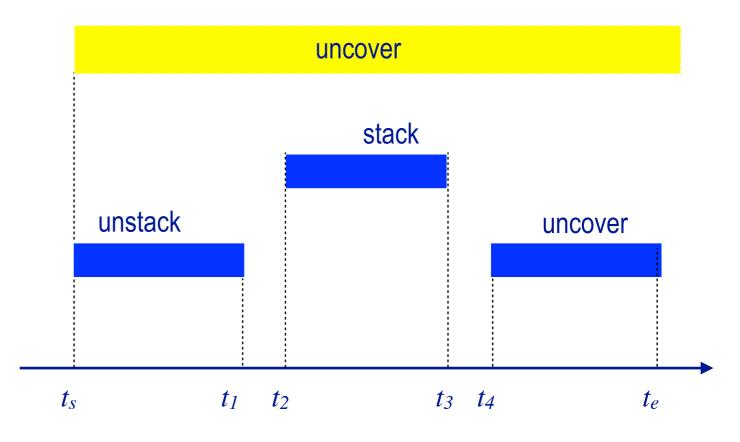
 $[t_s, t_s + 1] \operatorname{top}(p) = c'$

 $[t_s, t_s + 1]grip(k) = empty$

constraints: attached(k, d), attached(p, d)

 $attached(p',d), p \neq p', c' \neq c$

 $t_1 \le t_2, \ t_3 \le t_4$



Chronicles

- Chronicle $\phi = (A, S_T, T, C)$
 - A: temporally qualified actions and tasks
 - S_T : a priori supported assertions
 - T: temporally qualified assertions
 - C: constraints
- lacktriangledown ϕ represents
 - Current state and future predicted events
 - Tasks to be performed
 - Assertions and constraints to be satisfied
 - => planning problems and (partial) plans

Chronicles

Initial chronicle

```
\phi_0:
```

tasks: [t, t']bring(r, c1, dock4)

supported: $[t_s]loc(r1) = dock1$

 $[t_s]loc(r2)=dock2$

 $[t_s + 10, t_s + \delta]$ docked(ship1)=dock3

 $[t_s]$ top(pile1)=c1

 $[t_s]$ pos(c1)=pallet

assertions: $[t_e]loc(r1) = dock1$

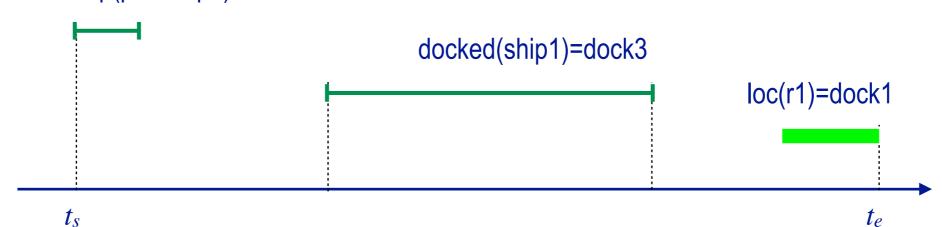
 $[t_e]$ loc(r2) = dock2

constraints: attached(pile1,ship1)

$$t_s < t < t' < t_e$$
, $20 \le \delta \le 30$, $t_s = 0$

bring(r, c1, dock4)

loc(r1)=dock1
top(pile-ship1)=c1

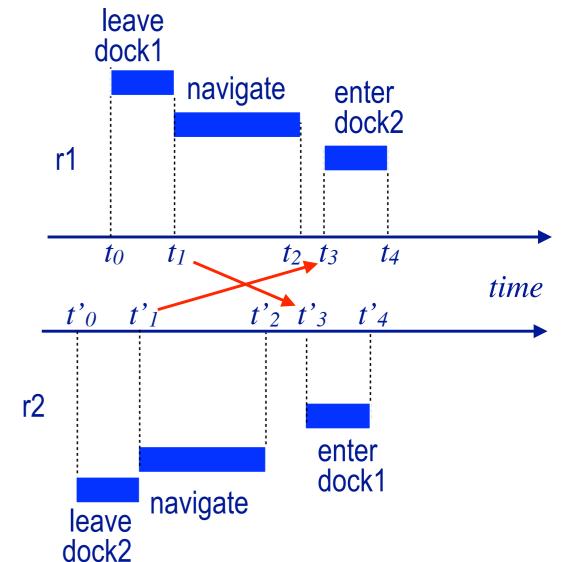


Chronicles

Partial plan

 ϕ :

tasks: $[t_0, t_1]$ leave(r1,dock1,w1) $[t_1, t_2]$ navigate(r1,w1,w2) $[t_3, t_4]$ enter(r1,dock2,w2) $[t'_0, t'_1]$ leave(r2,dock2,w2) $[t'_1, t'_2]$ navigate(r2,w2,w1) $[t'_3, t'_4]$ enter(r2,dock1,w1)



supported: $S_{\mathcal{T}}$

assertions: \mathcal{T}

constraints: $t'_1 < t_3, \ t_1 < t'_3, \ t_s < t_0$ $t_s < t'_0, \ t_4 < t_e, \ t'_4 < t_e$

adjacent(dock1,w1), adjacent(dock2,w2) connected(w1,w2)

Outline

- ✓ Introduction
- √ Representation
- Temporal planning
 - Resolvers and flaws
 - Search space
- Consistency and controllability
- Acting with executable primitives
- Acting with atemporal refinement
- Conclusion

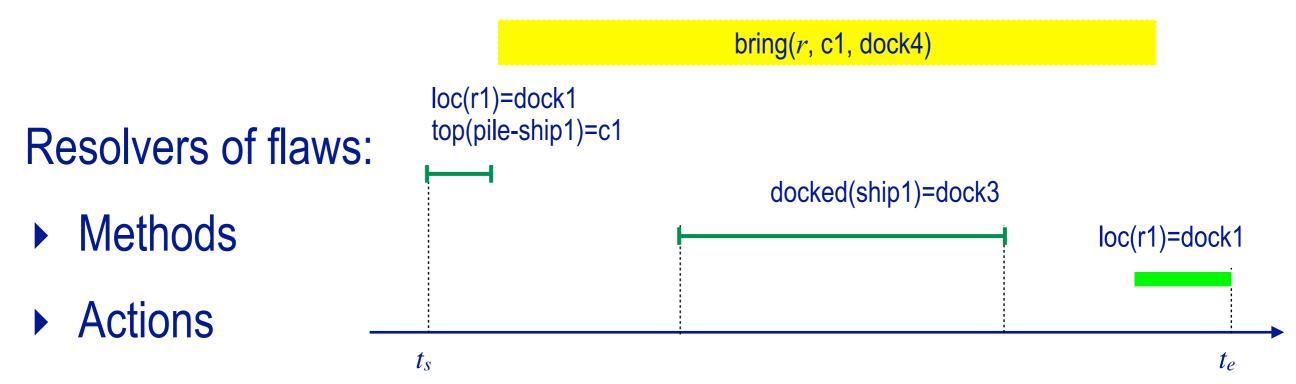
Temporal Planning

Starting from an *initial chronicle*:

- Refine into primitive actions
- Add causal supports to
- Add separation constraints for

nonrefined tasks
nonsupported assertion
conflicting assertions

flaws



Persistence assertions and constraints

Temporal Planning

A chronicle ϕ is a valid solution plan iff

- \bullet does not contain nonrefined tasks
- all assertions in ϕ are causally supported, either by supported assertions initially in ϕ_0 or by assertions from methods and primitives in the plan
- the chronicle ϕ is secure

no conflicting assertions in consistant instances

Temporal Planning

```
TemPlan(\phi, \Sigma)
   Flaws \leftarrow \text{set of flaws of } \phi
   if Flaws = \emptyset then return \phi
   arbitrarily select f \in Flaws
   Resolvers \leftarrow \text{set of resolvers of } f
   if Resolvers=0 then return failure
   nondeterministically choose \rho \in Resolvers
   \phi \leftarrow \mathsf{Transform}(\phi, \rho)
   Templan(\phi, \Sigma)
```

Combines in CSP-based approach

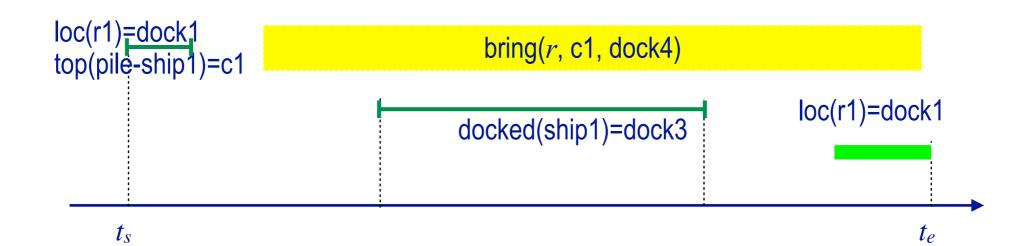
- task decomposition planning
- plan-space planning
- temporal planning

Resolvers for flaws

Resolver for a nonrefined task in ϕ : an instance m of a method applicable to the task s.t. all the constraints of m are consistent with those of ϕ .

Transforming $\phi = (\mathcal{A}, \mathcal{S}_{\mathcal{T}}, \mathcal{T}, \mathcal{C})$ with resolver m:

- replace in \mathcal{A} the task by the subtasks and actions of m
- add the assertions of m and those of the primitives in m either to $\mathcal{S}_{\mathcal{T}}$ if these assertions are causally supported or to \mathcal{T}
- add to \mathcal{C} the constraints of m and those of its actions.



Resolvers for flaws

Nonsupported assertions in $\phi = (\mathcal{A}, \mathcal{S}_{\mathcal{T}}, \mathcal{T}, \mathcal{C})$: those initially in ϕ_0 plus those from the refinement of tasks and the insertion of actions

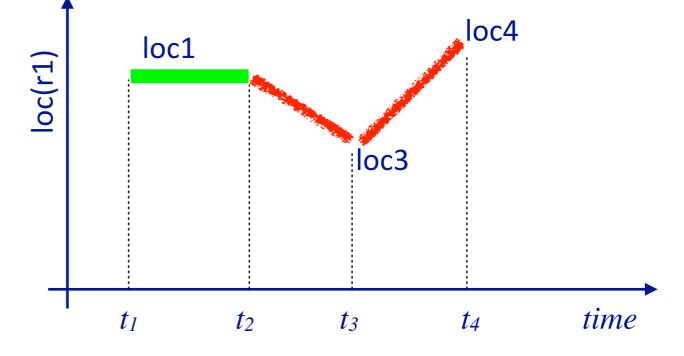
Different ways to support an assertion $\alpha \in \mathcal{T}$:

ullet add in ${\mathcal C}$ constraints on object and temporal variables

• add a persistence assertion in $\mathcal{S}_{\mathcal{T}}$

 \bullet add in \mathcal{A} a task or an action that brings an assertion

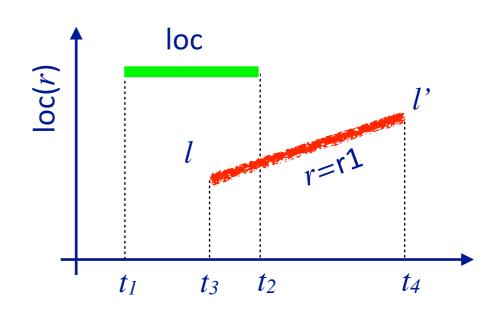
supporting α



Resolvers for flaws

Flaws due to conflicting assertions handled incrementally by maintaining ϕ a secure chronicle:

- Detect possible conflicts for each new assertion in ϕ
- Find sets of separation constraints consistent with the constraints in current ϕ
- Add separation constraints to ϕ



Search Space

- Planning search space: a directed graph
 - Node: a chronicle ϕ
 - Edge (ϕ, ϕ') : ϕ' =Transform (ϕ, ϱ) , ϱ resolver for flaw in ϕ
 - Acyclic graph
 - Not necessarily finite
- Heuristics
 - Flaw with smallest numbers of resolvers (as in *variable-ordering*)
 - Resolver the least constraining to current ϕ (as in *value-ordering*)
 - Elaborate heuristics based on domain transition graphs and reachability graphs
- ▶ Critical operation: maintain consistency of *C*

Outline

- ✓ Introduction
- √ Representation
- √ Temporal planning
- Consistency and controllability
 - Object constraints
 - Temporal constraint
 - Controllability of an STNU
- Acting with executable primitives
- Acting with atemporal refinement
- Conclusion

Consistency

Object constraints maintained by Templan

$$l \neq loc2, l \in \{loc3, loc4\}$$

 $r = r1, o \neq o$ '
 $loc(r) \neq l$ '

Temporal constraints maintained by Templan

$$a < t$$
 $t < t$
 $a \le t - t \le b$

Possibly coupled constraints

=> Assume no coupled constraint

Object Constraint

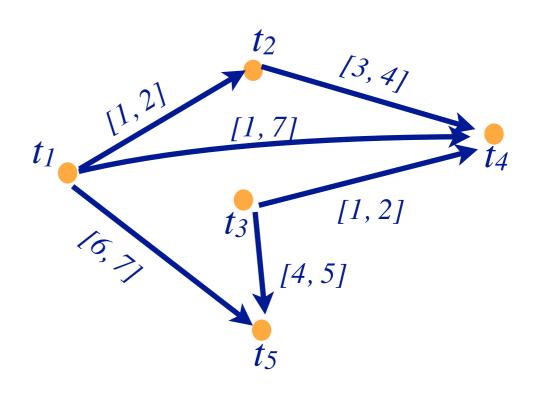
- Unary and binary constraints on object variables
 due to binding and separation constraints and rigid relations
- Corresponds to maintaining the consistency of a general CSP over finite domains => NP-complete problem
- Incremental arc or path consistency algorithms
 - Not complete, but efficient trade-off for filtering inconsistent instances
 - Do not reduce the completeness of the algorithm, just prune fewer nodes in search tree
- Combined with complete algorithms, e.g., forward-checking on the free variables remaining in the final plan

Temporal Constraints

Simple temporal networks (STN)

$$a \le t_j - t_i \le b$$

notation $r_{ij} = [a,b]$
entails $r_{ji} = [-b,-a]$



STN

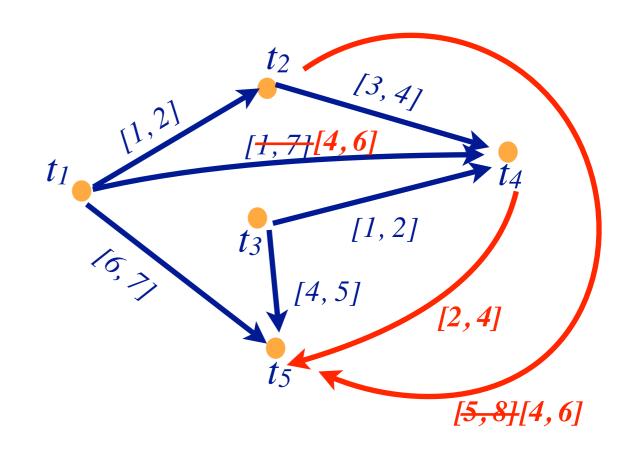
- Incrementally synthesized by Templan starting from ϕ_0
- Incrementally instantiated at acting time
- Maintained consistent throughout planning and acting

Temporal Constraints

Simple temporal networks (STN)

$$a \le t_j - t_i \le b$$

notation $r_{ij} = [a,b]$
entails $r_{ji} = [-b,-a]$



Constraint propagation rules

Conditions	Propagated constraint
$t_1 \xrightarrow{[a,b]} t_2 , t_2 \xrightarrow{[a',b']} t_3$	$t_1 \xrightarrow{[a+a',b+b']} t_3$
$t_1 \xrightarrow{[a,b]} t_2 , t_1 \xrightarrow{[a',b']} t_2$	$t_1 \xrightarrow{[max\{a,a'\},min\{b,b'\}]} t_2$

$$r_{12} \cdot r_{23}$$
 $r_{12} \cap r'_{12}$

Temporal Constraints

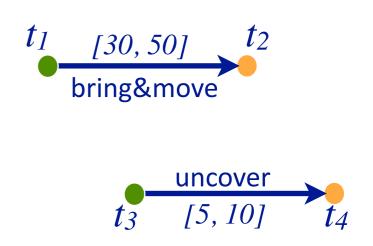
Path consistency algorithm

```
PC(\mathcal{V}, \mathcal{E}) for each k: 1 \leq k \leq n do for each pair i, j: 1 \leq i < j \leq n, i \neq k, j \neq k do r_{ij} \leftarrow r_{ij} \cap [r_{ik} \bullet r_{kj}] if r_{ij} = \emptyset then return inconsistent
```

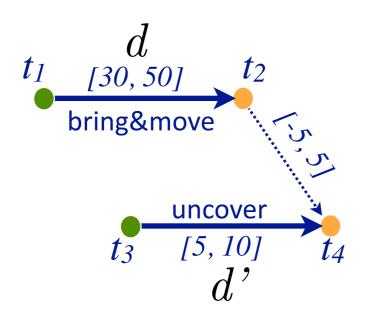
- Algorithm complete
- Returns a minimal network when consistent
- Complexity in time $O(n^3)$, incremental update in $O(n^2)$

Controllability

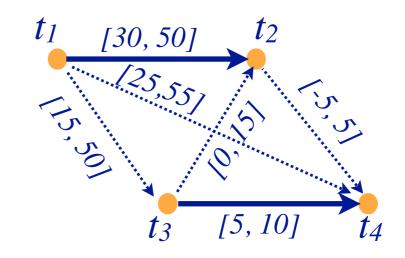
- Controllable vs contingent time points
 - t_1 and t_3 : controllable
 - t₂ and t₄: contingent
 random variables that are known
 to satisfy some constraints
- PC cannot be allowed to constrain a contingent time point
- Even if minimal network does not constrain any contingent time point the corresponding plan may not be feasible



Controllability



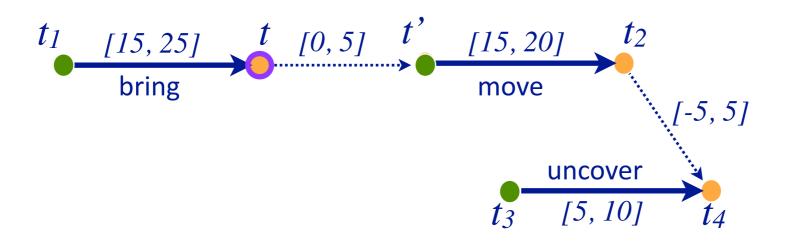
minimal network



$$d - d' - 5 \le t_3$$

$$t_3 \le d - d' + 5$$

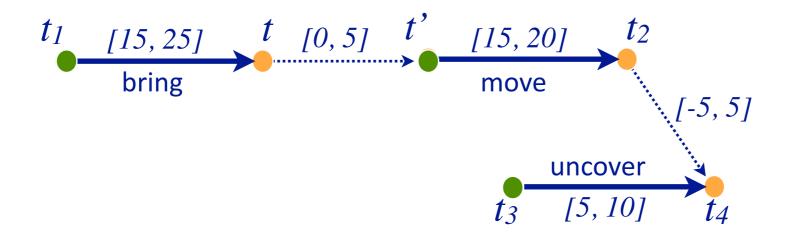
$$\Rightarrow 40 \le t_3 \le 25 !!$$



observe t assign t' at any moment after t in [0, 5] assign t_3 10 units after t'

- Simple temporal network with uncertainty (STNU)
 - Controllable and contingent time points
 - Constraints, as in STN, controllable and contingent
- Controllable STNU: there exist values for controllable points that meets all constraints
 - Strong controllability: solution works for all possible values of contingent points in their predicted intervals
 - Weak controllability: solution as a function of the values of contingent points, if known in advance
 - *Dynamic controllability*: solution that is built dynamically, for each controllable point given the *observation* of past contingent points

- ▶ A dynamic execution strategy for an STNU: online procedure for assigning, in some order, a value to each controllable point t, (i.e., triggering commands at right moment)
 - such that all controllable constraints are met, and
 - given that the values of all contingent variables preceding t are known and fit their assumed constraints
- An STNU is *dynamically controllable* if there exists a dynamic execution strategy for it
- Assigning a value to controllable t = triggering a command

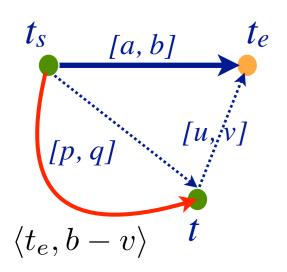


observe t assign t' at any moment after t in [0, 5] assign t_3 10 units after t'

Checking dynamic controllability of an STNU

- For a chronicle $\phi = (A, S_T, T, C)$ temporal constraints in C correspond to an STNU
- TemPlan: maintains incrementally STNU dynamically controllable
 - If Path Consistency reduces a contingent constraint
 => not dynamically controllable
 - Otherwise: test of dynamic controllability as an extension of Path Consistency with additional constraint propagation rules

Dynamic Controllability Checking



if u < 0 and $v \ge 0$ then t should wait until either $t_s + b - v$ or t_e occurs

Constraint propagation rules

Conditions	Propagated constraint
$t_s \xrightarrow{[a,b]} t_e , \ t \xrightarrow{[u,v]} t_e , \ u \ge 0$	$t_s \xrightarrow{[b',a']} t$
$t_s \xrightarrow{[a,b]} t_e , t \xrightarrow{[u,v]} t_e , u < 0 , v \ge 0$	$t_s \xrightarrow{\langle t_e, b' \rangle} t$
$t_s \xrightarrow{[a,b]} t_e , t_s \xrightarrow{\langle t_e,u \rangle} t$	$t_s \xrightarrow{[min\{a,u\},\infty]} t$
$t_s \xrightarrow{\langle t_e, b \rangle} t , t' \xrightarrow{[u,v]} t$	$t_s \xrightarrow{\langle t_e, b' \rangle} t'$
$t_s \xrightarrow{\langle t_e, b \rangle} t , t' \xrightarrow{[u,v]} t , t_e \neq t$	$t_s \xrightarrow{\langle t_e, b-u \rangle} t'$

$$a' = a - u, b' = b - v$$

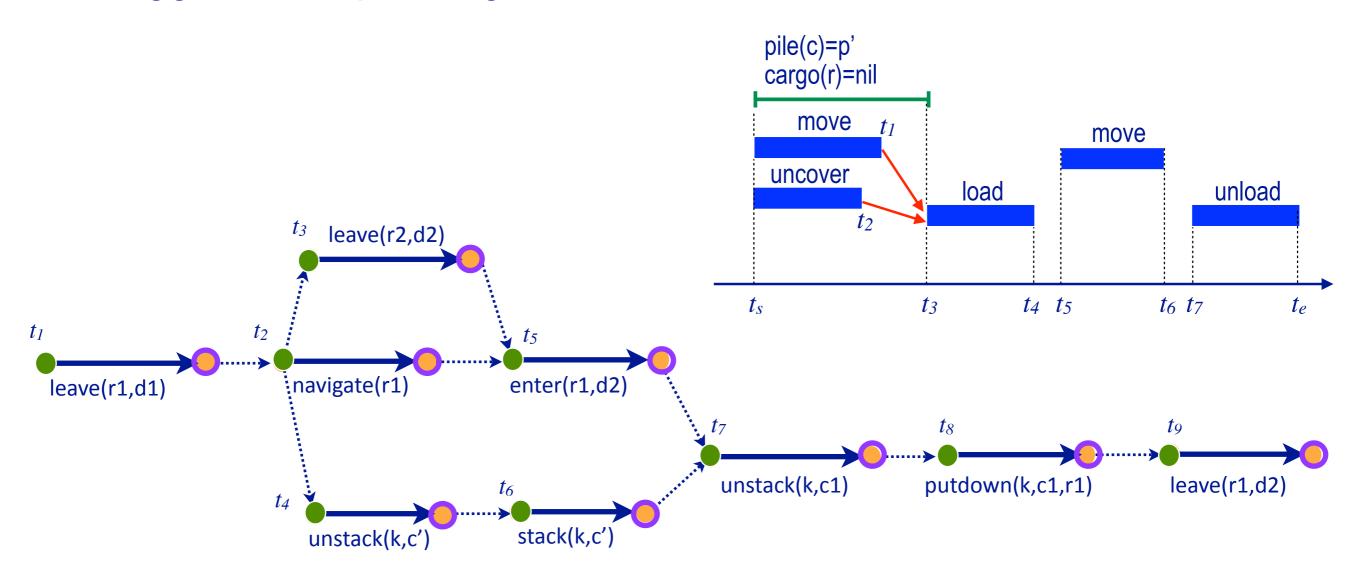
Outline

- ✓ Introduction
- √ Representation
- √ Temporal planning
- √ Consistency and controllability
- Acting with executable primitives
 - Dispatching
 - Observation actions
- Acting with atemporal refinement
- Conclusion

Dispatching Algorithm

Problem

- Given a dynamically controllable plan with executable primitives
- Trigger corresponding commands from online observations



Dispatching Algorithm

Plan grounded in realtime: when constrained w.r.t. absolute bounds or when execution starts

- Future point t is bounded with absolute bounds $[l_t, u_t]$
- Past point is instantiated

A controllable time point t that remains in the future

- t is alive if the current time $now \in [l_t, u_t]$
- t is enabled if
 - t is alive,
 - for every precedence constraint t' < t, t' has occurred, and
 - for every wait constraint $\langle t_e, \alpha \rangle$, either t_e has occurred or α has expired

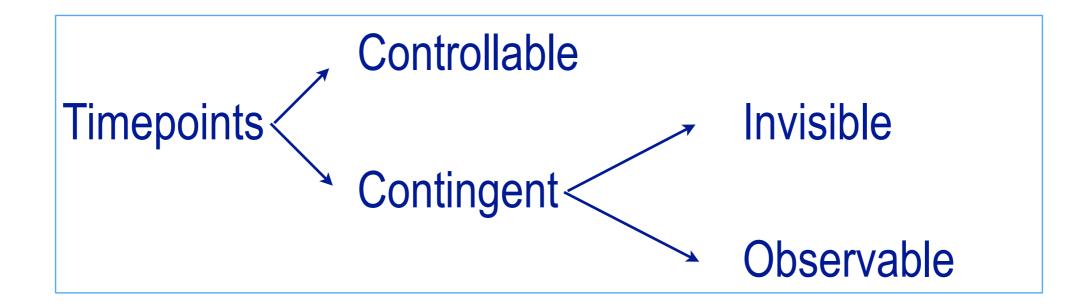
Dispatching Algorithm

```
\mathsf{Dispatch}(plan)
  initialize the network
  while there are controllable points that have not occurred do
         update now
         update contingent points that have been observed
         enabled \leftarrow set of enabled points
         for every t \in enabled such that now = u_t do
                trigger t
         arbitrarily choose other points in enabled; trigger them
         propagate in the network the values of triggered points
```

Temporal monitoring

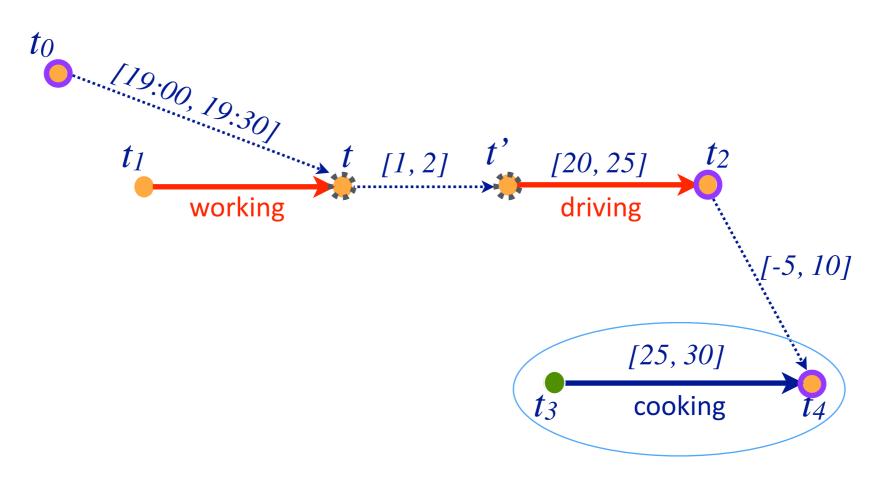
Observation Actions

- ▶ Assumption: all occurrences of contingent events are observable
 - Observation needed for dynamic controllability
 - In general not all events are observable
- Refining STNU into POSTNU



▶ Is POSTNU dynamically controllable ?

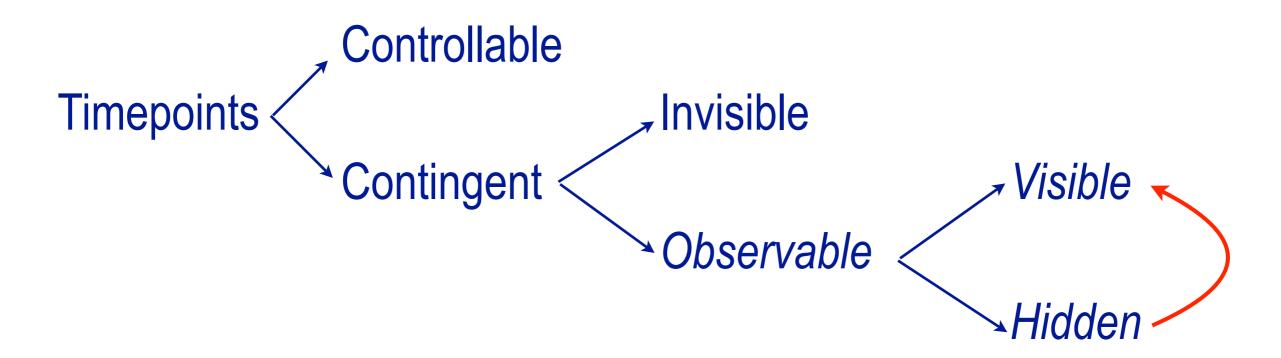
Observation Actions



- Controllable
- Contingent { Invisible observable

Observation Actions

- ▶ POSTNU dynamically controllable if there exists an execution strategy that chooses future controllable points to meet all the contraints, given the observation of past *visible* points
- ▶ Observable ≠ visible
 - Observable means it will be known when observed
 - It can be temporarily hidden



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Atemporal Refinement of Primitive Actions

- Planning primitives are compound tasks at the acting level
- Refined into commands with refinement methods in RAE

```
\begin{array}{ll} \operatorname{m-leave}(r,d,w,e) \\ \operatorname{task:} \ \operatorname{leave}(r,d,w) \\ \operatorname{pre:} \ \operatorname{loc}(r) = d, \operatorname{adjacent}(d,w), \operatorname{exit}(e,d,w) \\ \operatorname{body:} \ \operatorname{until} \ \operatorname{empty}(e) \ \operatorname{wait}(1) \\ \operatorname{goto}(r,e) \end{array} \qquad \begin{array}{ll} \operatorname{Operational} \\ \operatorname{model} \end{array}
```

Descriptive model

```
\begin{aligned} & \operatorname{leave}(r,d,w) \\ & \operatorname{assertions:} \ [t_s,t_e] \operatorname{loc}(r){:}(d,w) \\ & [t_s,t_e] \operatorname{occupant}(d){:}(r,\operatorname{empty}) \\ & \operatorname{constraints:} \ t_e \leq t_s + \delta_1 \\ & \operatorname{adjacent}(d,w) \end{aligned}
```

Atemporal Refinement of Primitive Actions

- Planning primitives are compound tasks at the acting level
- Refined into commands with refinement methods in RAE

```
\begin{array}{l} \text{m-unstack}(k,c,p) \\ \text{task: unstack}(k,c,p) \\ \text{pre: pos}(c) = p, \text{top}(p) = c, \text{grip}(k) = \text{empty} \\ \text{attached}(k,d), \text{attached}(p,d) \\ \text{body: locate-grasp-position}(k,c,p) & \text{Operational} \\ \text{move-to-grasp-position}(k,c,p) & \text{model} \\ \text{grasp}(k,c,p) \\ \text{until firm-grasp}(k,c,p) & \text{ensure-grasp}(k,c,p) \\ \text{lift-vertically}(k,c,p) \\ \text{move-to-neutral-position}(k,c,p) \end{array}
```

Atemporal Refinement

Pros

- Simple online refinement with RAE
- Avoids breaking down uncertainty of contingent duration
- Can be augmented with temporal monitoring functions in RAE e.g., watchdogs, methods with duration preferences

Cons

Does not handle temporal requirements at the command level,
 e.g., concurrency synchronization

Summary

- Rich chronicle representation with temporal refinement
- Planning with chronicle refinement
- Consistency and controllability
- Acting with chronicle dispatching and refinement

- ANML modeling language
- FAPE Acting and Planning Environment

Conclusion

- Temporal models enrich descriptive and operational models of actions
- Chronicle-based approach very flexible for integrating generative and task decomposition techniques
- Acting refinement methods can be extended to integrate temporal construct of chronicles

```
action uncover (containers c, piles p){
 [start] c.in == p;
 :decomposition \{[all] p.top == c; \};
 :decomposition {
  constant (...);
  [start] p.top == prevtop;
  p!= otherp; c!= prevtop;
  k.attached == d; p.ondock == d;
  otherp.ondock ==d;
  [all] p.available == true;
  [all] otherp.available == true;
  [all] contains {
  s1: unstack(k,prevtop,p);
  s2: stack(k,prevtop,otherp);
  s3: uncover(c,p);};
  end(s1) \le start(s2);
  end(s2) \le start(s3);
```

Example: dwr

```
action goto (robots r, docks to){
 constant docks from;
 constant waypoints wa, wb;
  [start] r.loc == from;
 :decomposition {from == to; };
 :decomposition {from != to;
  adjacent(from, wa);
  adjacent(to, wb);
  [all] contains {
   s1: leave(r, from, wa);
   s2: navigate(r, wa, wb);
   s3 : enter(r, to, wb) ;};
  end(s1) \le start(s2);
  end(s2) \le start(s3);;
```

Example: search tree

