## Parallel Model Checking

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Parallel Model Checking



- Introduction
- Multiprocessor Computer Architecture
- State Space Construction
- Considerations



## **Model Checking**



**Model Checking :** Automatic System Analysis.

#### Verification :

- System Description
  - Behavior.
  - Architecture.
- Desired Property.
- Counter-Example.

## Model Checking

#### Definition

*Model Checking* : Given a Kripke structure M = (S, R, L) that represents a finite-state concurrent system and a temporal logic formula *f* expressing some desired specification, find the set of all states in *S* that satisfy  $f : \{s \in S \mid M, s \models f\}$ 

#### Two steps :

- State Space Construction (Kripke structure)
- Property Verification ({ $s \in S \mid M, s \models f$ })



## Flynn's Taxonomy of Computer Architecture

#### Notion of a stream of information :

SISD : single-instruction single-data





## Flynn's Taxonomy ...

 SIMD : single-instruction multiple-data  MIMD : multiple-instruction multiple-data







## **MIMD** Architecture

#### **Shared Memory :**



#### **Distributed Memory :**





## SUN FIRE X4600 M2

#### Brutus :

- Shared Memory
- 8 Processors Dual Core AMD Opteron
- NUMA : Non-Uniform Memory Access
- Minimum hop distance : Enhanced Twisted Ladder



Enhanced Twisted Ladder



## State Space Construction

#### **Complexity :**

- Irregular Problem
- Size is unknown by advance
- The model under consideration is a key performance issue



## State Space Construction ...

#### Three stereotypical types of model[Ezekiel08] :





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#### Parallel Model Checking

## **Related Work - SIMD**

#### State Space construction on a SIMD Machine :

- Caseli 1994
- Function Decomposition Model
  - Transition Firing
  - Reachability Graph Construction
    - Search Action
    - New State Creation



## **Related Work - MIMD Distributed Memory**

#### **Distributed State Space Generation**

- Ciardo97m, Hoverkor99, Lerdo 99, Caseli99, Hubert01
- Message Passing Interface (MPI)
- Objective : Expand Memory
- All threads executes same program in parallel

### Complexity

- Balance Workload
- Minimize Communication (Overhead)



## **Related Work - MIMD Distributed Memory**

### Partition Function is :

- *Proc* :  $S \Rightarrow \{0, ..., N-1\}$
- Proc(s) is the owner of state s

#### And must have :

- Spatial Balance
- Locality
- Temporal Balance



## **Related Work - MIMD Distributed Memory**

#### Partition Function can be :

- Static (User Provided)
- Oynamic

#### Example of a Partition Function :

• 
$$M = \{PL_1, PL_2, ..., PL_n\}$$

• 
$$C_s = \{PL_1, PL_5, PL_7\}$$

• 
$$(\#PL_1 + q * \#PL_5 + q^2 * \#PL_7) \mod N$$

- $\#PL_n$  = number of tokens at place  $PI_n$
- q is a prime number



## **Related Work - MIMD Distributed Memory**

### First Approximation :

- Orzan05
- Small approximation based on a set of abstraction interpretation





## **Related Work - MIMD Shared Memory**

### **Complexity :**

- Data Consistency
- Synchronization
- Thread Creation Overhead
- Bus Contention
- Data Race
- False Sharing



## Related Work - MIMD Shared Memory

- Global Shared Storage Data
- Allmeier97 :
  - Storage Structure : Balance Tree with Splitting in advance
- Inggs02 :
  - Work Stealing



## Considerations

#### **Objectives :**

- Bigger Models
- Speed up

#### **Problematics**

- Temporal Balance
- Memory Location



## Storage Structure

#### 1 - Global Storage Structure :

- Iow complexity
- better "all case" temporal balance
- irregular memory distribution
- synchronization and locks overhead





## Storage Structure

# 1 - Local Storage Structure per processor :

- high complexity (Partition Function)
- worst "all case" temporal balance
- uniform memory distribution



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#### Mixed of Distributed and Shared Solution :

- Local Storage Structures
- Small amount of shared memory
- Heuristic Policies for On-the-fly Temporal Balance





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