



# Simple is Beautiful: a Comparison-based Diagnosis

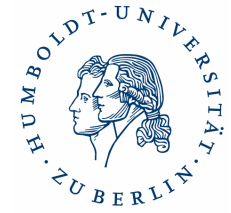
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*Venue: Sofitel Chicago Water Tower  
Chicago  
June 25, 2010*

# Outline

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Introduction

Comparison Model (with comparators)

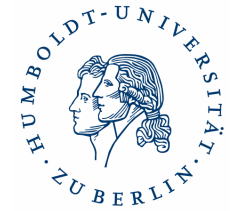
MM - Models

Key extensions

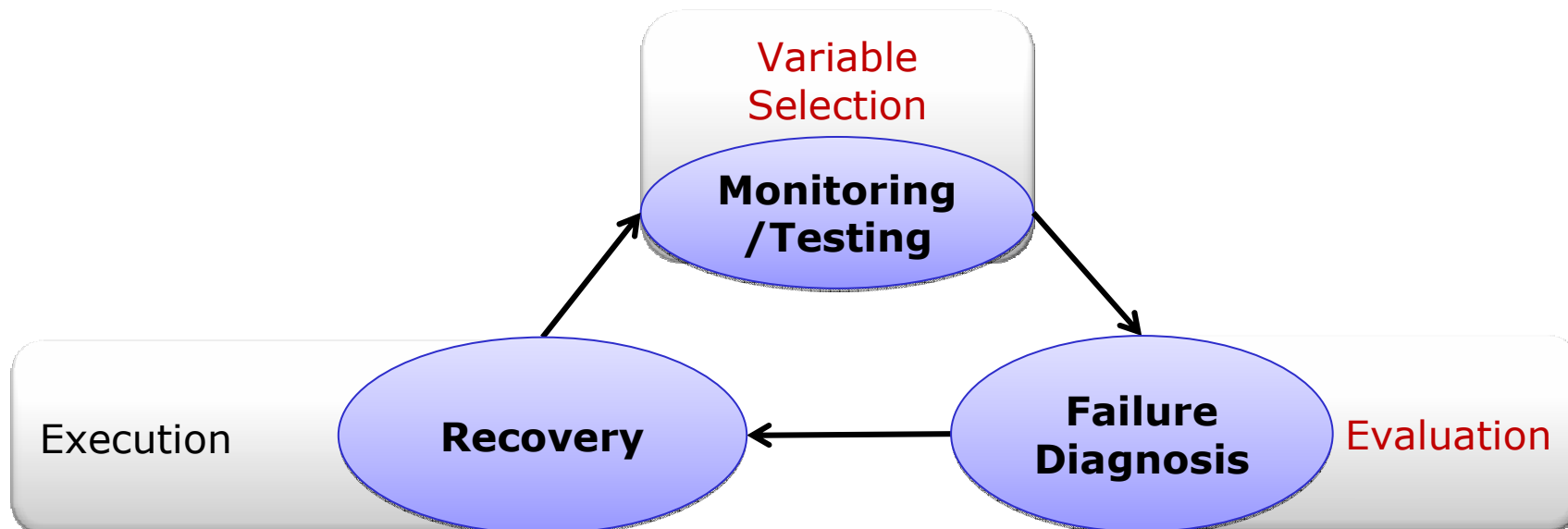
Implementations

Challenges

# Failure Diagnosis in Cycle

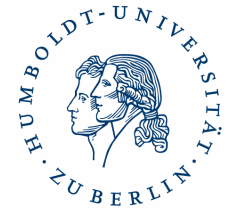


Failure diagnosis is an essential part of fault management and is usually followed by recovery actions.



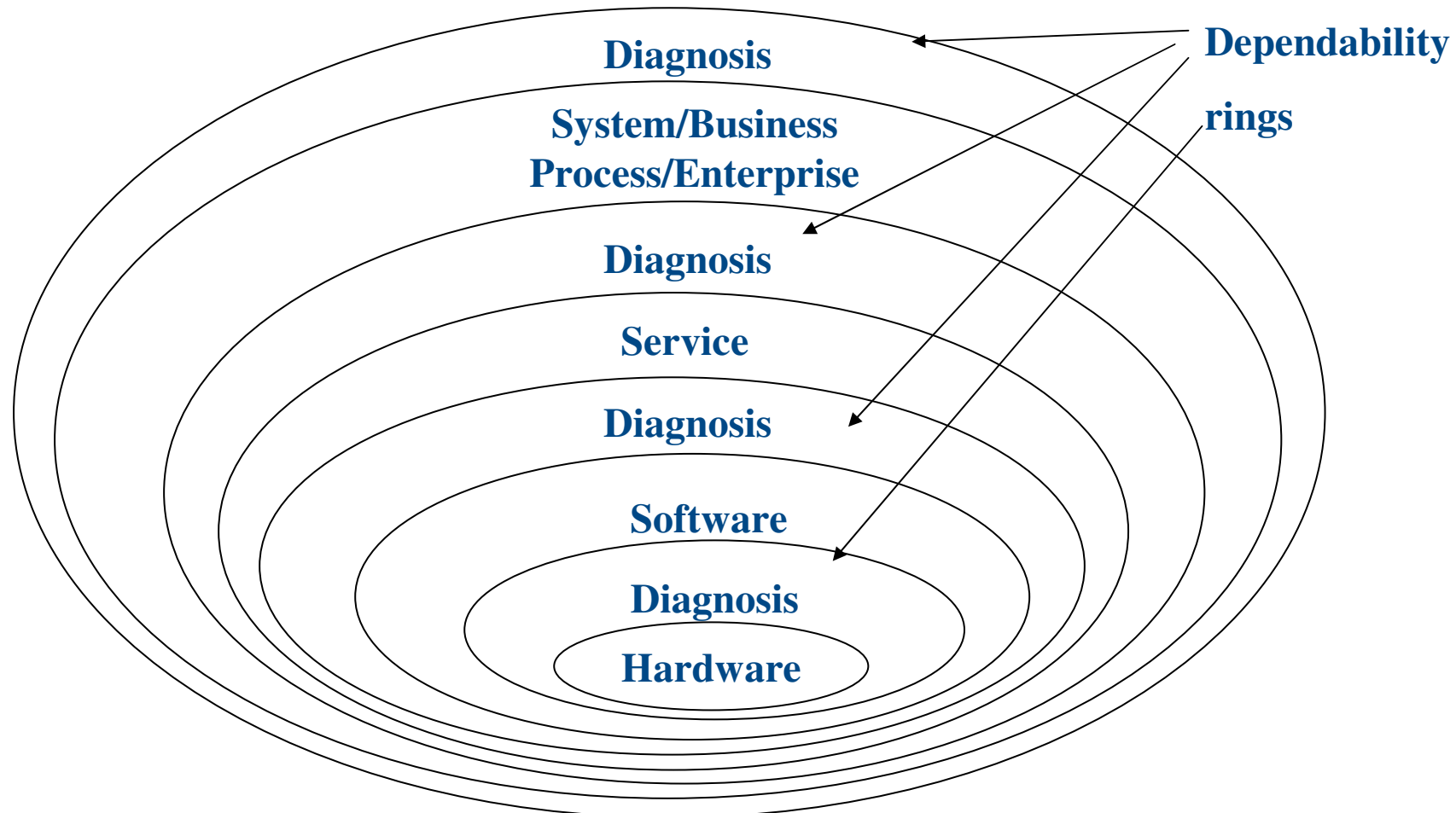
# *Failure Diagnosis (continued)*

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- Packaging, testability, diagnosability and performance instrumentation are frequently afterthoughts or are developed independently in the design process
- Use of concurrent error detection is frequently indispensable (especially in multiprocessor/cloud environments) due to high system complexity and rapid system contamination
- Diagnosis should cover all system levels
- In this talk: **Emphasis on application (algorithmic) and system level diagnosis**

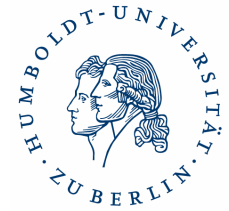
# Translucency – Getting the Biggest Bang for the Buck



At what level providing measures and mechanisms for diagnosis and proactive fault management will maximize the payoff (minimize downtime)?

# *Three Phenomena that Won't Go Away*

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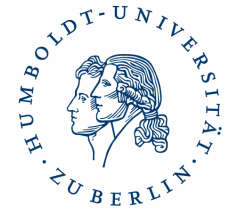


- Ever-increasing systems **complexity**
  - Growing connectivity, chip density and interoperability
  - Growing number of functionalities
- Increasing **uncertainty**
  - Ever-growing number of attacks and threats, novice users and third-party or open-source software, COTS
  - Ever new failure modes
  - Dynamicity (frequent configurations, reconfigurations, updates, upgrades and patches, ad hoc extensions)
- Increasing real-**time** requirements
  - Systems proliferation to applications in all domains of human activity where many of them require real time
  - Growing users expectations regarding timeliness

Therefore, diagnosis is and will remain a permanent challenge.

# *The Key Principle: KISS*

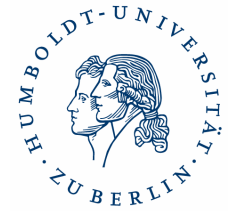
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- With ever-increasing systems complexity **simplicity** is of an essence
- Striving for **simplicity** and keeping all stages of the system design and development simple is a major challenge
- Divide-and-conquer, integration, interoperability and structured design principles and hierarchical approaches should be applied to all aspects of design and maintenance. These main methods are insufficiently exploited design of various functionalities/properties such as testability, diagnosis, real time, performance monitoring, etc.
- In this talk the focus is on enforcing simplicity in system diagnosis

# *The Comparison*

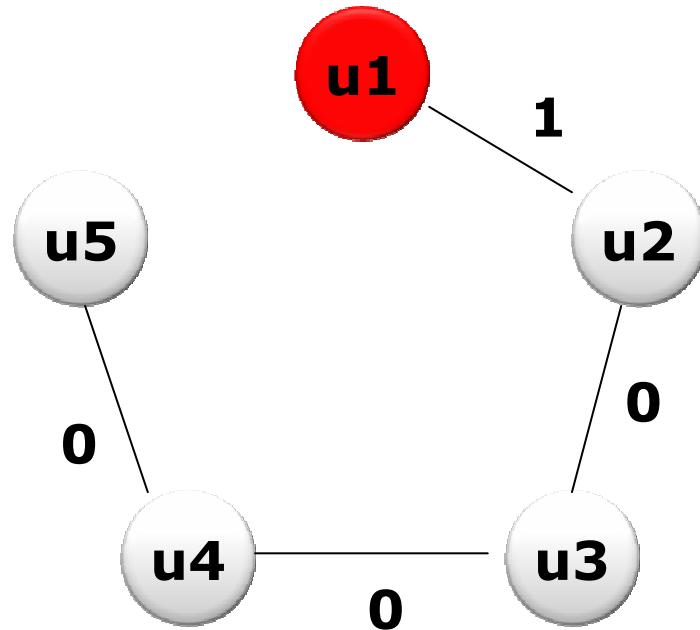
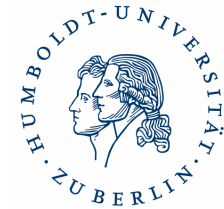
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- The comparison is an essential concept from beginning of times
- In computers the comparison is widely used:
  - Password
  - Bank account, identity checking
  - Signatures, counters, results of computations
  - Testing and diagnosis, watchdogs, etc.
- First fault-tolerant systems have used comparison in duplex system for failure detection
- Examples include AT&T's ESS and 3B20 system series



# Basic Comparison Models



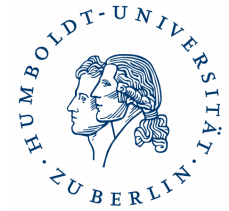
Unit 1	Unit 2	Comparison Outcome
fault-free	fault-free	0 (pass)
fault-free	faulty	1 (fail)
faulty	fault-free	1 (fail)
faulty	faulty	1 (fail) or X

- Each edge corresponds to a comparator
- $\lfloor (n+1)/2 \rfloor$  comparators (node cover) guarantee detection
- $n-1$  comparators are sufficient for a single node diagnosis
- $n(n-1)/2$  comparators assure  $(n-2)$ -diagnosability ( $t=n-2$ )

(Malek, 1980, Chwa and Hakimi, 1981)

# *Definition of t-Diagnosability*

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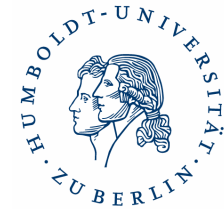
A system of  $n$  units is one step  $t$ -fault diagnosable ( $t$ -diagnosable) if all faulty units within the system can be located without replacement, provided the number of faulty units does not exceed  $t$ .

1.  $2t+1 \leq n$
2. At least  $t$  units must test each unit

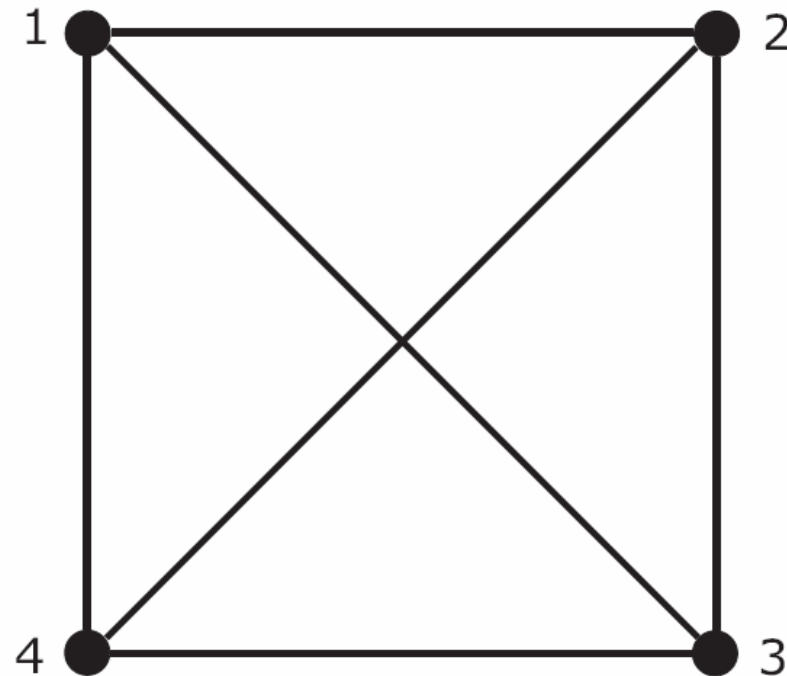
(Preparata-Metze-Chien)

- Several diagnosis algorithms have been proposed, with a variety of assumptions

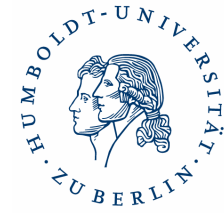
# Diagnosability in a Comparison Model



- Edges indicate comparators between pairs of units
- A complete graph is  $(n-2)$ -diagnosable for  $n > 3$
- In general,  $n - \lfloor n/3 \rfloor$  comparators (for  $n > 2$ ) are sufficient for diagnosis under a single fault assumption and up to  $n$  nodes fault detection

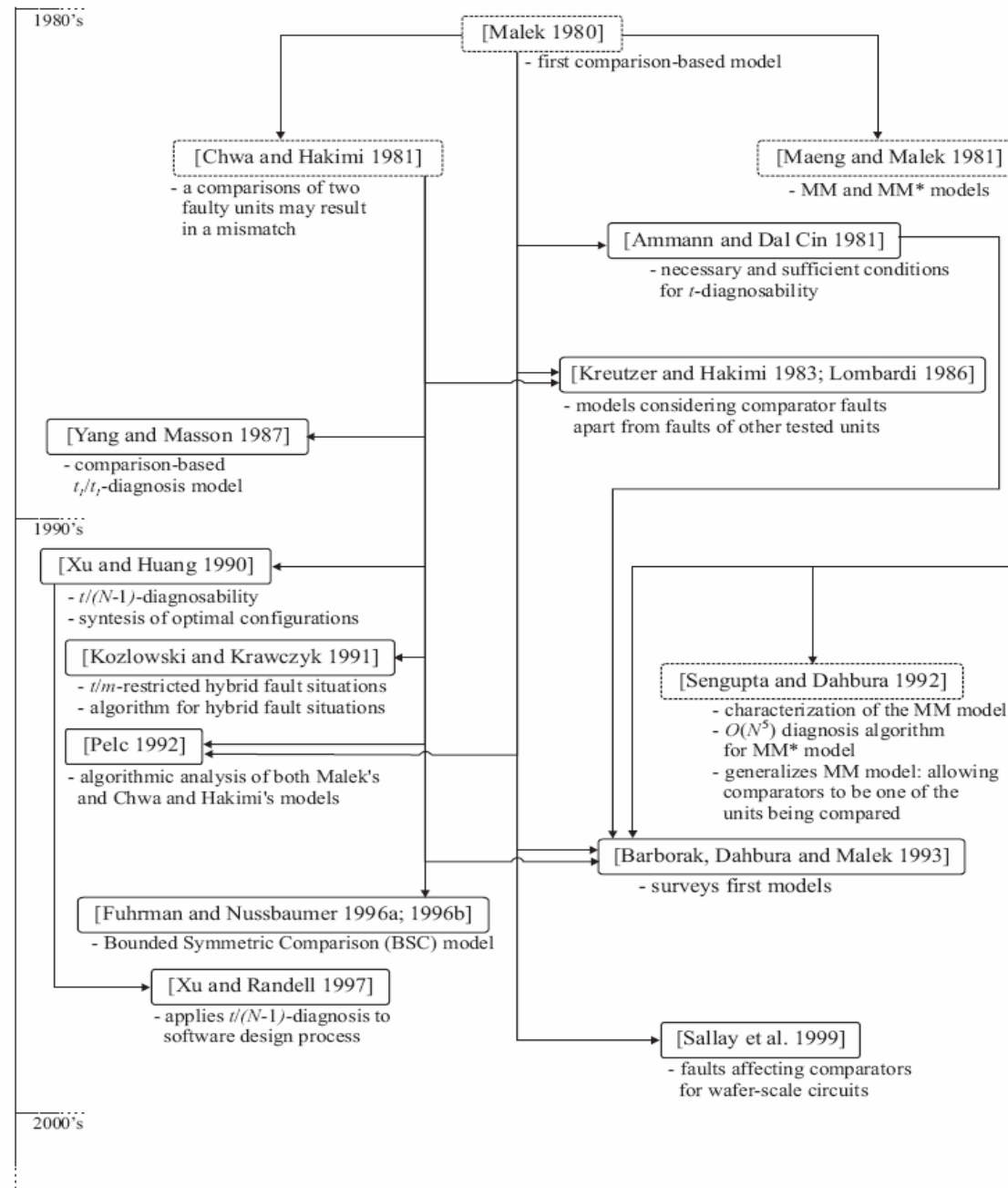


An example graph representing comparisons among four units



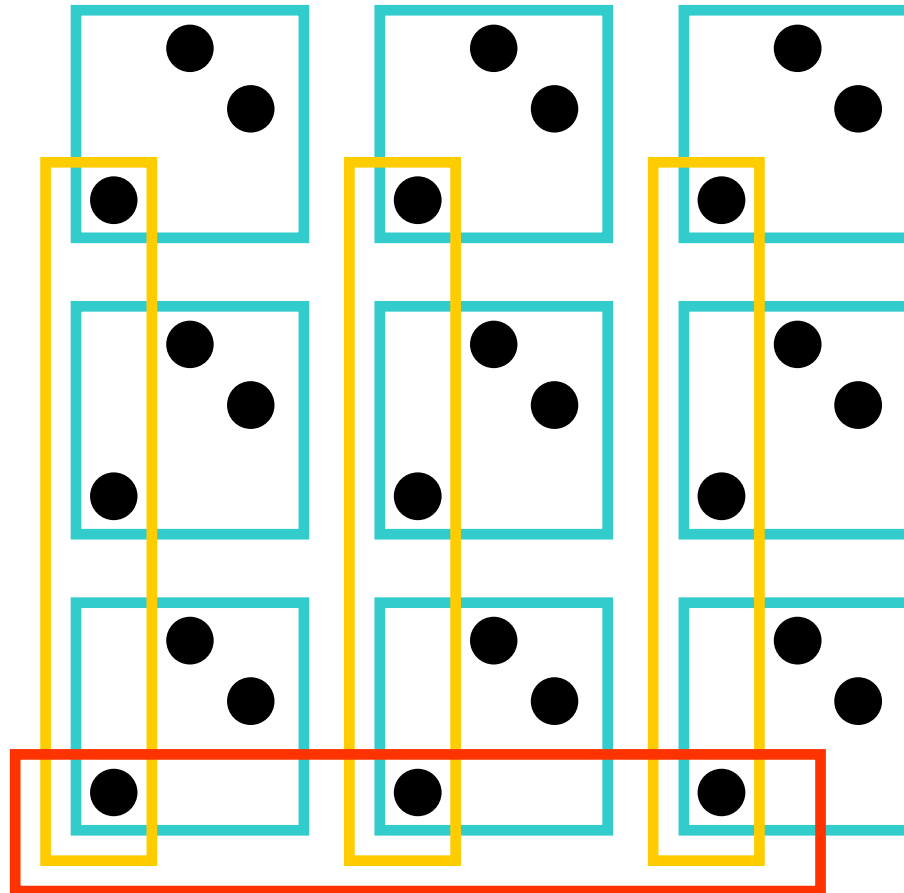
Model	Reference	Main Contributions
Malek's model	[Malek 1980]	<ul style="list-style-type: none"> <li>- first comparison-based model</li> <li>- compared units are different</li> <li>- the comparison of one or two faulty units results in a mismatch</li> <li>- central observer is a trusted unit that executes comparisons and performs the diagnosis</li> <li>- the diagnosability is <math>N - 2</math></li> </ul>
	[Ammann and Dal Cin 1981]	<ul style="list-style-type: none"> <li>- necessary and sufficient conditions for <math>t</math>-diagnosability</li> </ul>
	[Sallay et al. 1999]	<ul style="list-style-type: none"> <li>- strategy to identify faults affecting comparators</li> <li>- application for wafer-scale circuits</li> </ul>
	[Pelc 1992]	<ul style="list-style-type: none"> <li>- algorithmic analysis of both Malek's and Chwa and Hakimi's models</li> <li>- worst case number of tests for optimal algorithms for <math>t</math>-diagnosis, sequential <math>t</math>-diagnosis and one-step <math>t</math>-diagnosis for both models, under non-adaptive and adaptive testing</li> </ul>
	[Barborak et al. 1993]	<ul style="list-style-type: none"> <li>- surveys early models</li> </ul>
Chwa and Hakimi's model	[Chwa and Hakimi 1981b]	<ul style="list-style-type: none"> <li>- the comparison of two faulty units may result in a match</li> </ul>
	[Fuhrman and Nussbaumer 1996b; 1996a]	<ul style="list-style-type: none"> <li>- Bounded Symmetric Comparison model, considers a limit on the number of faulty units that can produce identical results</li> </ul>
	[Kozłowski and Krawczyk 1991]	<ul style="list-style-type: none"> <li>- extension of Chwa and Hakimi's model for <math>t/m</math>-restricted hybrid fault situations</li> </ul>
	[Yang and Masson 1987]	<ul style="list-style-type: none"> <li>- comparison-based <math>t_1/t_1</math>-diagnosis model</li> </ul>
	[Xu and Huang 1990]	<ul style="list-style-type: none"> <li>- characterization of <math>t/(N - 1)</math>-diagnosability under Chwa and Hakimi's model</li> <li>- synthesis of optimal <math>t/(N - 1)</math>-diagnosable configurations for topologies such as chains and loops</li> </ul>
	[Xu and Randell 1997]	<ul style="list-style-type: none"> <li>- application of <math>t/(N - 1)</math> diagnosis to the software design process</li> </ul>
	[Kreutzer and Hakimi 1983; Lombardi 1986]	<ul style="list-style-type: none"> <li>- models considering comparator faults apart from faults of other tested units</li> <li>- characterization of the proposed models, <math>(t - t_c)</math>-diagnosability</li> </ul>

## Summary of comparison-based results based on early models from Duarte, Roverli, Ziwich, Albini, 2010

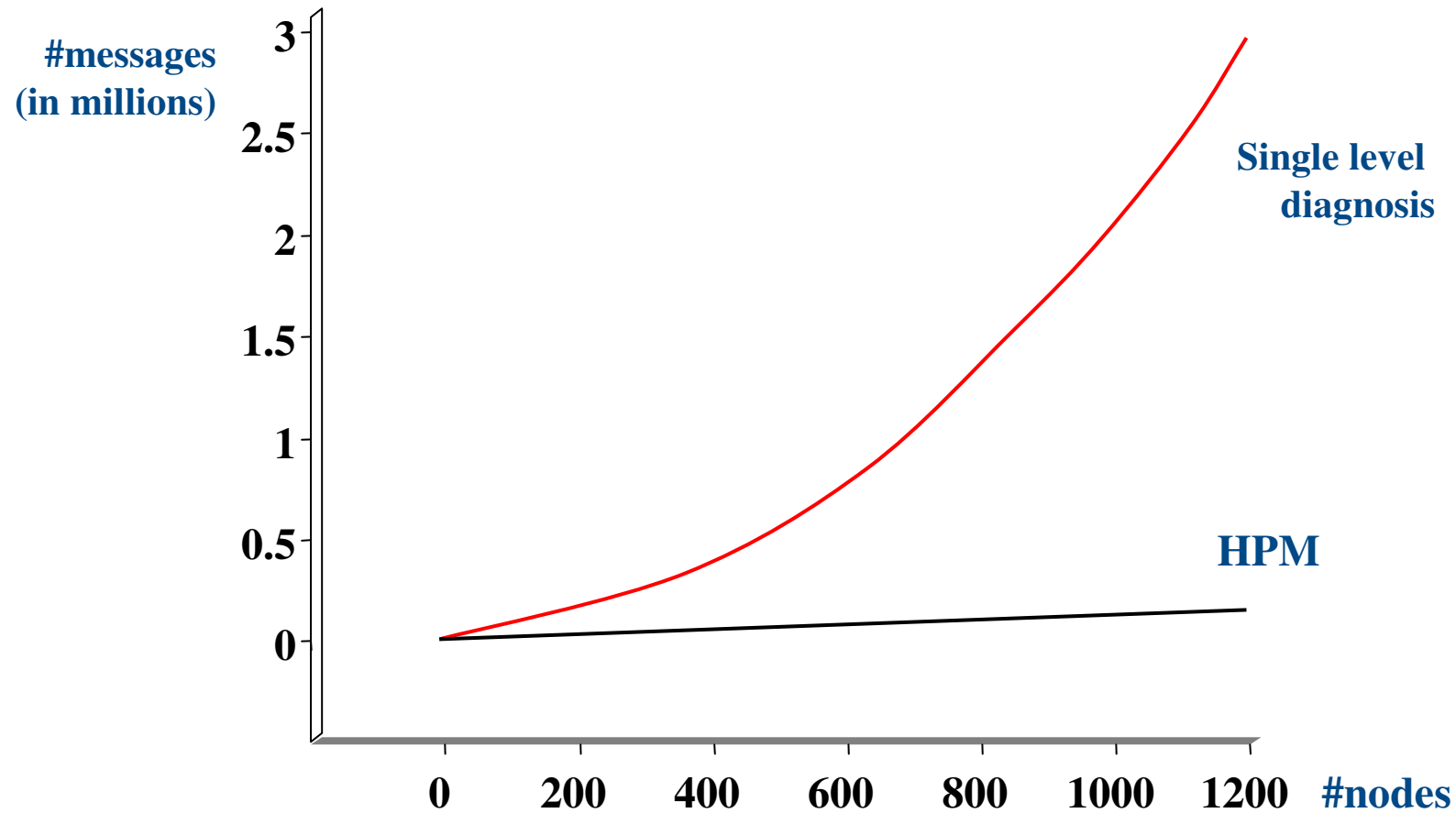
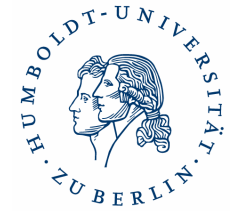


## Comparison-based diagnosis timeline: results based on early models from Duarte, Roverli, Ziwich, Albin, 2010

# Hierarchical Diagnosis



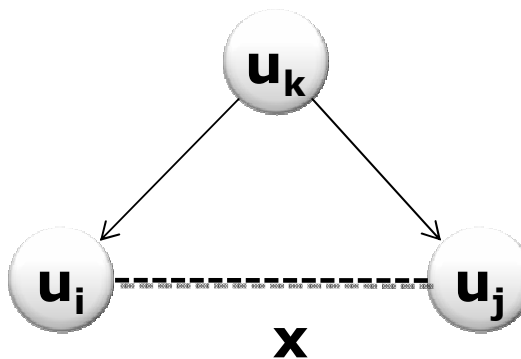
# The Hierarchical Diagnosis Performance



# The MM-Comparison Models (1981)



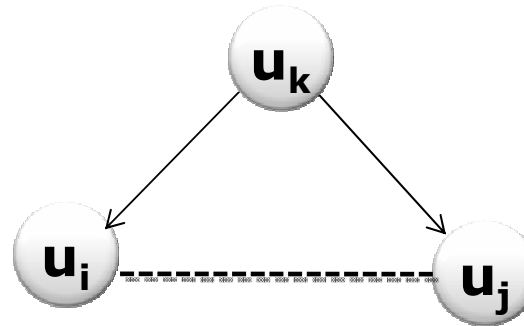
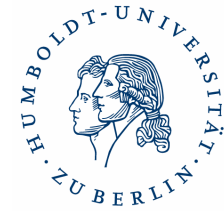
- A year later we have proposed a different approach:
  - The testing processor sends some test input to two adjacent nodes or asks for signature or counter values
  - The testing processor compares the two responses and sends the outcome to the central diagnosis unit
- The comparison graph is built where two nodes  $u_i$  and  $u_j$  are connected by an edge if there is a testing node  $u_k$  that tests  $u_i$  and  $u_j$ .
- Graph theory based algorithms can be used to identify the set of faulty processors



Maeng and Malek (1981)

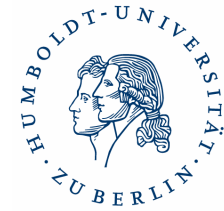


# MM-Comparison Model

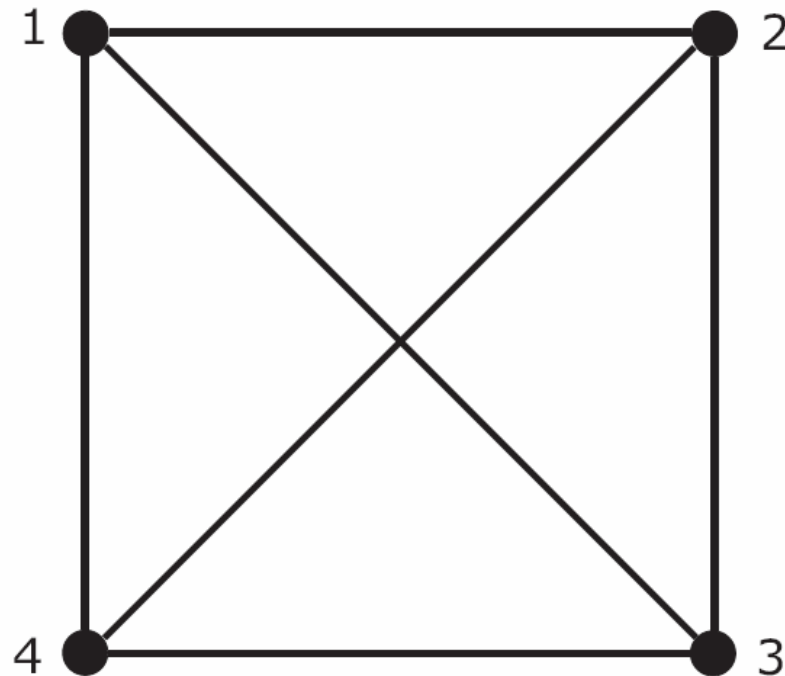


Comparator (Unit k)	Unit i	Unit j	Comparison Outcome
fault-free	fault-free	fault-free	0 (pass)
fault-free	fault-free	faulty	1 (fail)
fault-free	faulty	fault-free	1 (fail)
fault-free	faulty	faulty	1 (fail)
faulty	fault-free	fault-free	0 or 1
faulty	fault-free	faulty	0 or 1
faulty	faulty	fault-free	0 or 1
faulty	faulty	faulty	0 or 1

# Diagnosability in an MM-Model

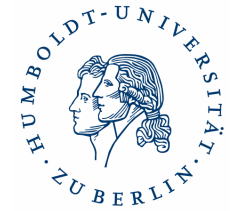


- Edges indicate connections in the system
- A graph is  $t$ -diagnosable iff  $d(v) > t-1$  and a condition on duals to prevent ambiguities
- Also an algorithms for generating an optimal graph for  $t > 3$  has been proposed

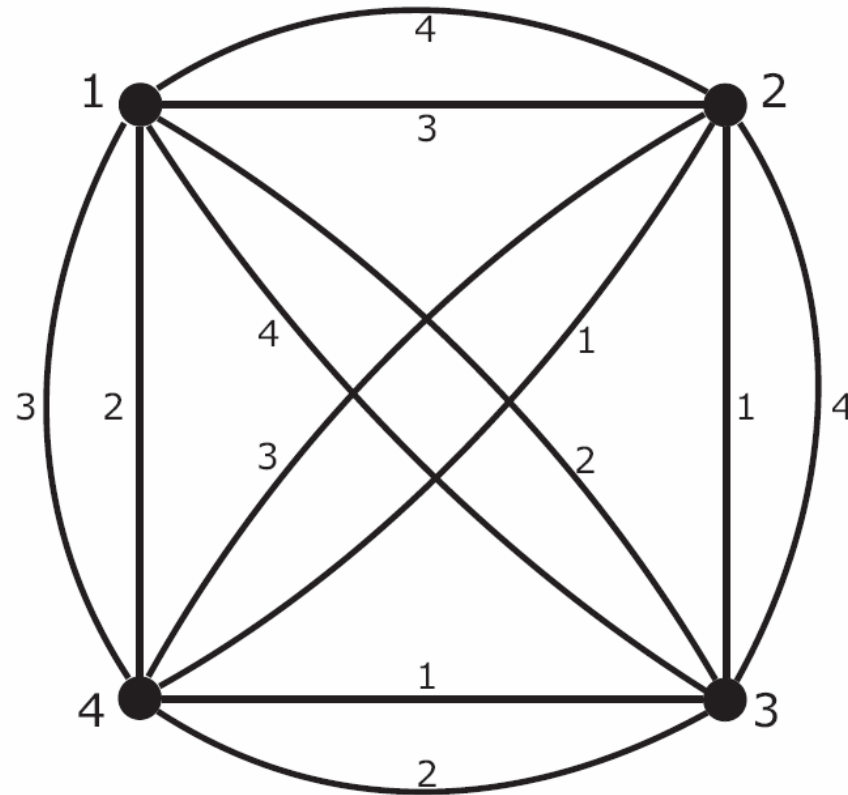


An example graph representing a system with four units

# MM Comparison Model



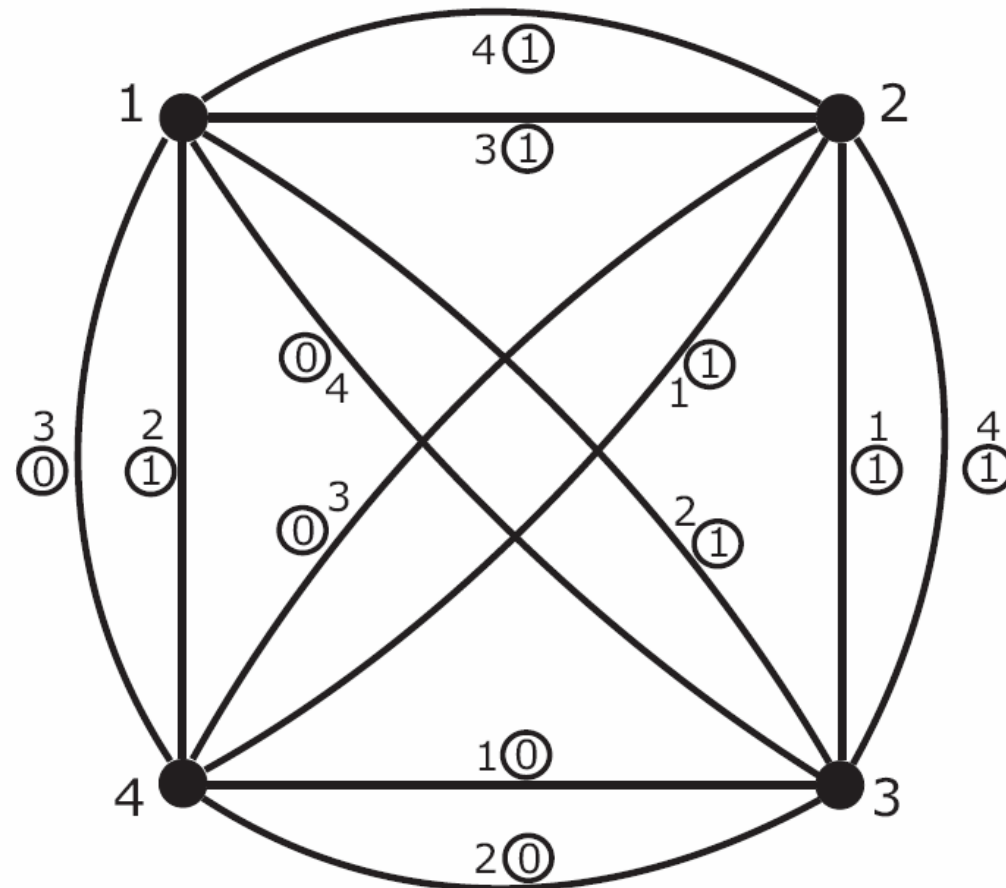
- The edges indicate comparisons between a specific pair of units
- Edge labels are id's of comparator units



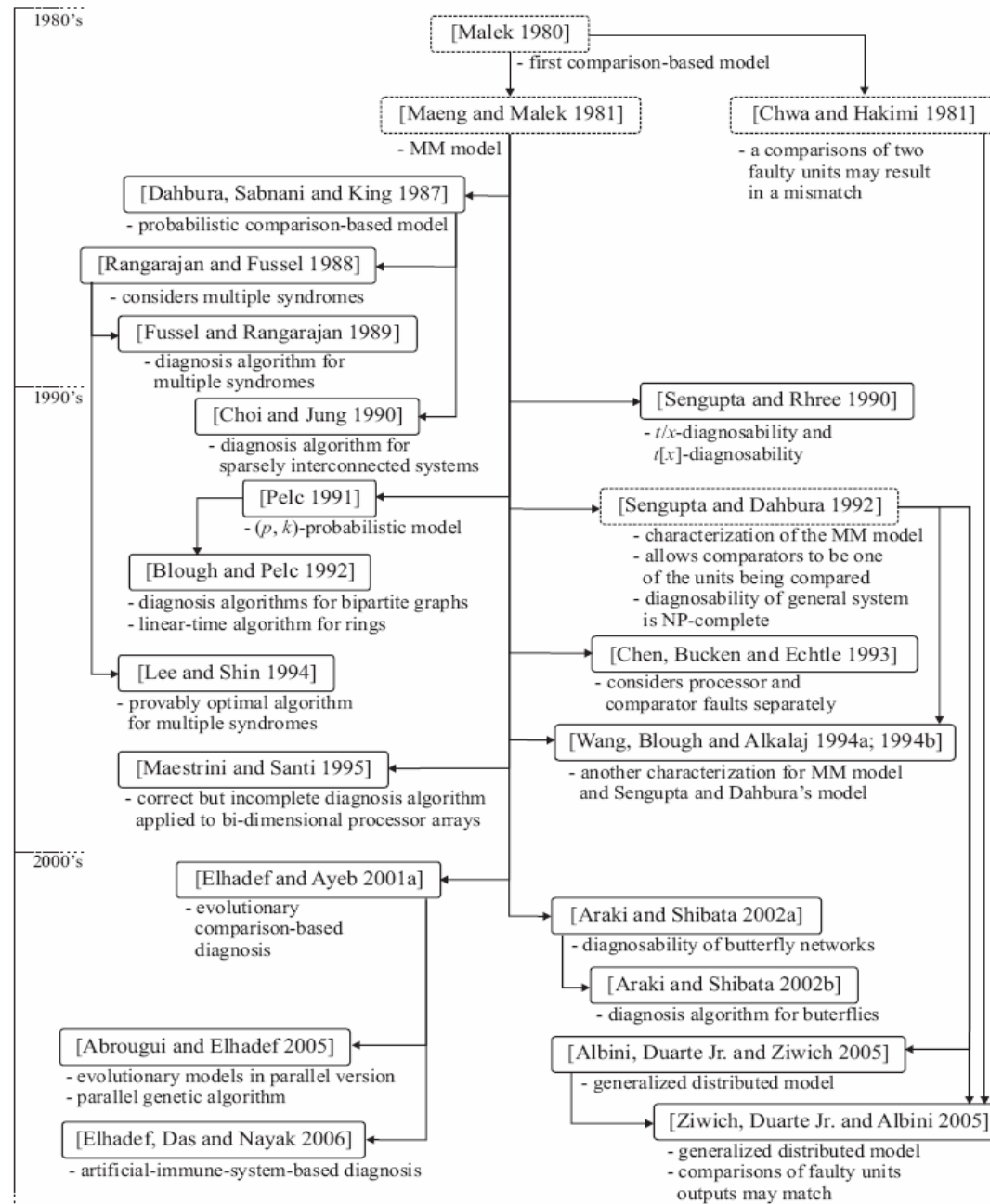
An MM-comparison multi-graph  $M$   
for a system with four units

# MM-Comparison Model

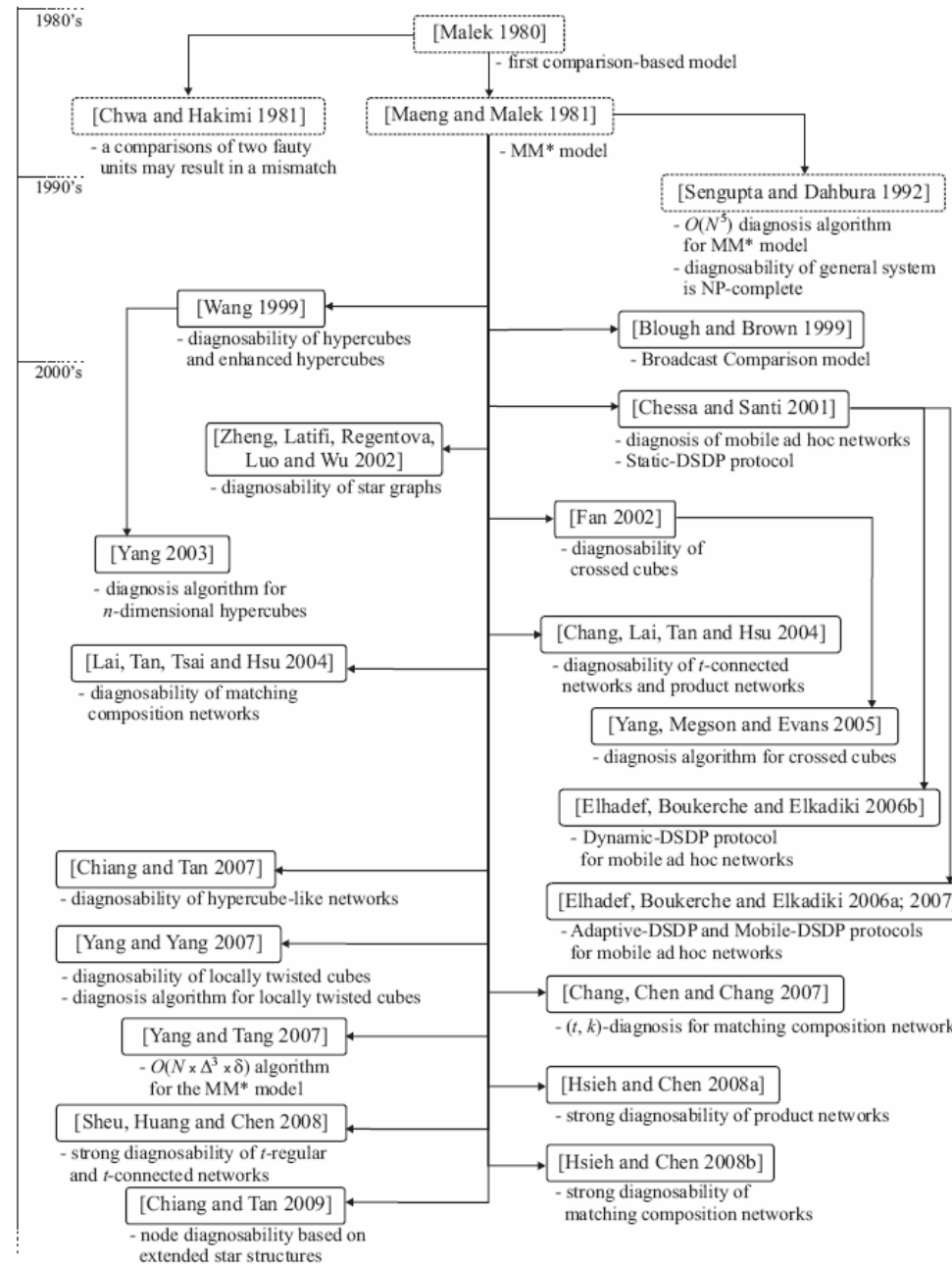
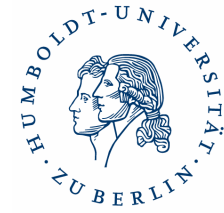
- Necessary and sufficient conditions for one-step diagnosability are given
- Algorithm for design of diagnosable systems has been proposed
- Polynomial diagnosis algorithms (e.g., Sengupta and Dahbura)



Multi-graph  $M$  depicts comparison outcomes for the example system



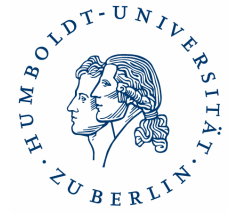
## Comparison-based diagnosis timeline: results based on the MM model from Duarte, Roverli, Ziwich, Albini, 2010



**Comparison-based diagnosis timeline: results based on the MM\* model  
from Duarte, Roverli, Ziwich, Albini, 2010**

# *Main Directions*

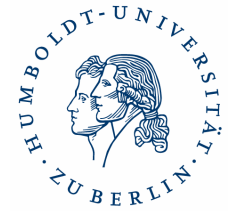
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- Variations on assumptions
- Diagnosis algorithms
- $t$ -diagnosability

# *Variations on assumptions*

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- Two faulty units may give identical outputs (Chwa and Hakimi)
- Probabilistic diagnosis (Masson, Dahbura et al)
- Distributed diagnosis (Kuhl and Reddy, ...)
- Reliability of communication
- Reliability of comparators/processors
- ...

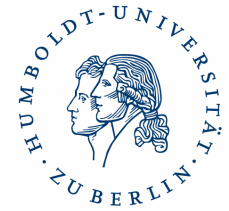
Bottom line:

Let's get a consensus on minimal and realistic assumptions



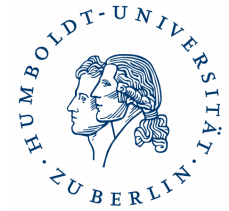
# Diagnosis algorithms

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- One-step and sequential diagnosis algorithms, centralized versus distributed
- $O(n^2)$  distributed algorithm for the basic model (Amman and Dal Cin)
- $O(n^5)$  diagnosis algorithm for the MM\* model plus NP-completeness result (Sengupta and Dahbura)
- $O(n d_{max}^3 d_{min})$  diagnosis algorithm (Yang and Tang)
- A number of other algorithms for specific topologies and applications (wireless)

# *t*-diagnosability

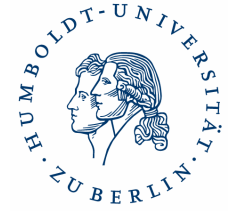


- Several special cases with respect to specific topologies (mesh, hypercube, twisted cube, butterfly, etc)
- Several result regarding variations on *t*-diagnosability
  - $t/(N-1)$ -diagnosability (Xu, Huang, Randell)
  - $t/m$ -diagnosability ( $m$  misleading comparisons, Krawczyk)
  - $t/x$ - and  $t/[x]$ -diagnosability ( $x$  missing c., Sengupta)
  - $t/s$  and  $t_1/t_1$ -diagnosability (up to  $s = t_1$  can be replaced, Friedman, Masson et al)

for either one-step or sequential diagnosability

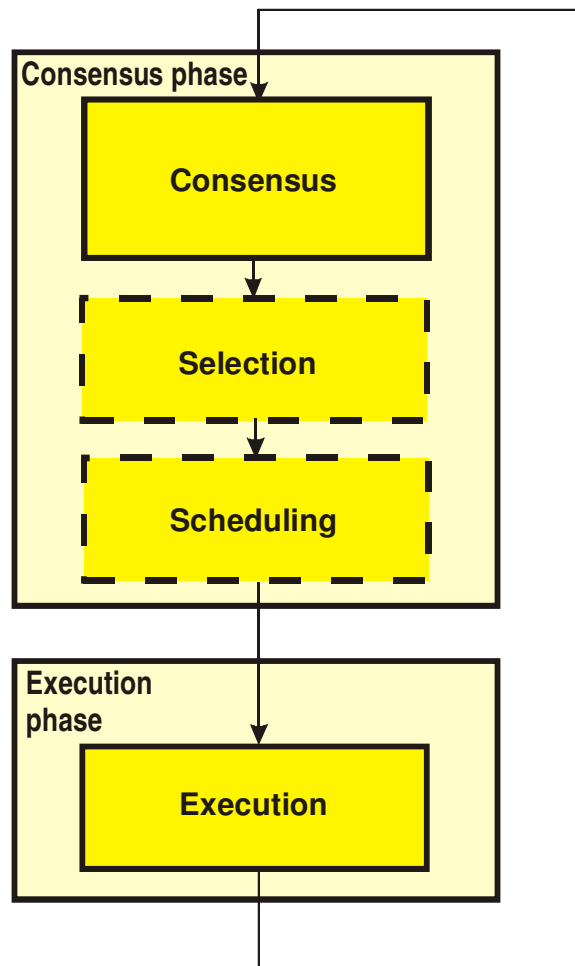
# *Implementations*

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- Large number of applications
- This summary is from a personal perspective

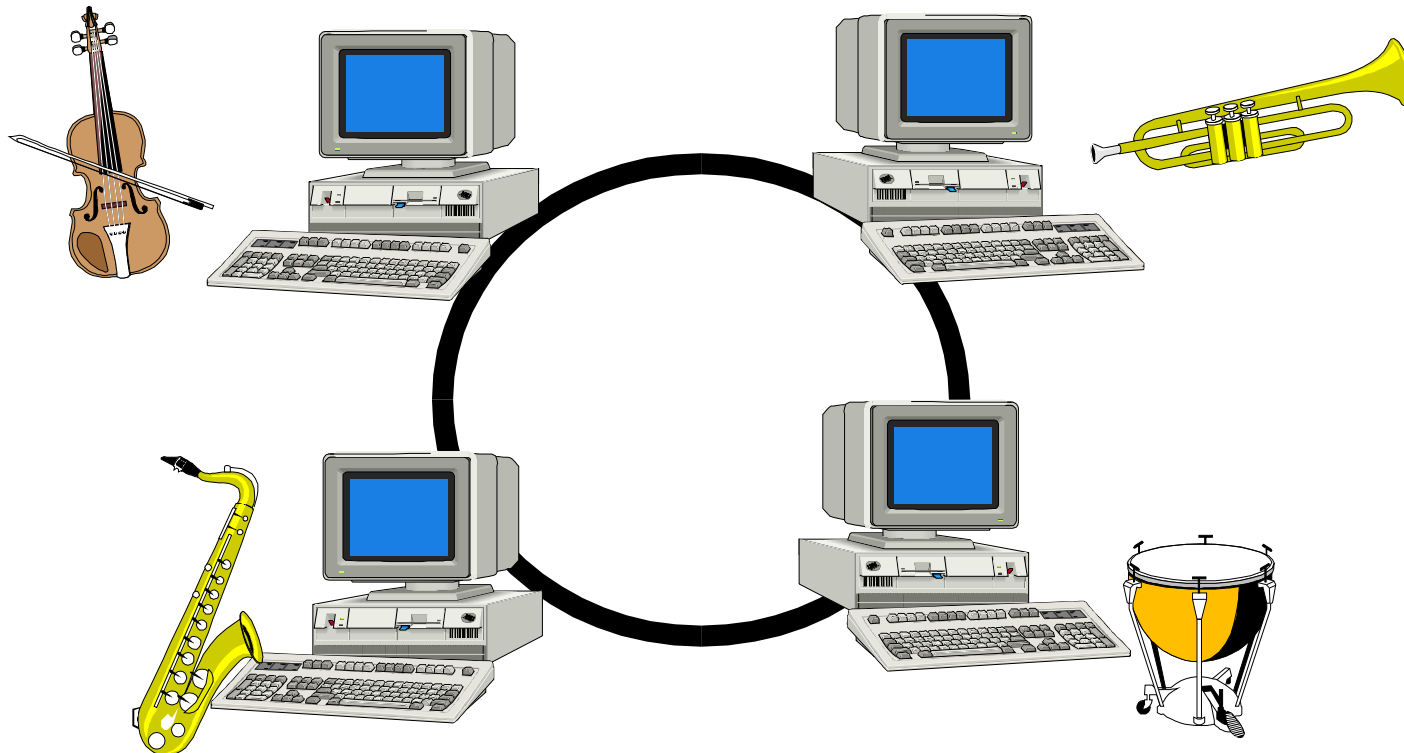
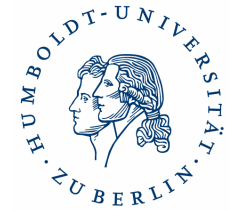
# CORE - COnsensus for REsponsiveness



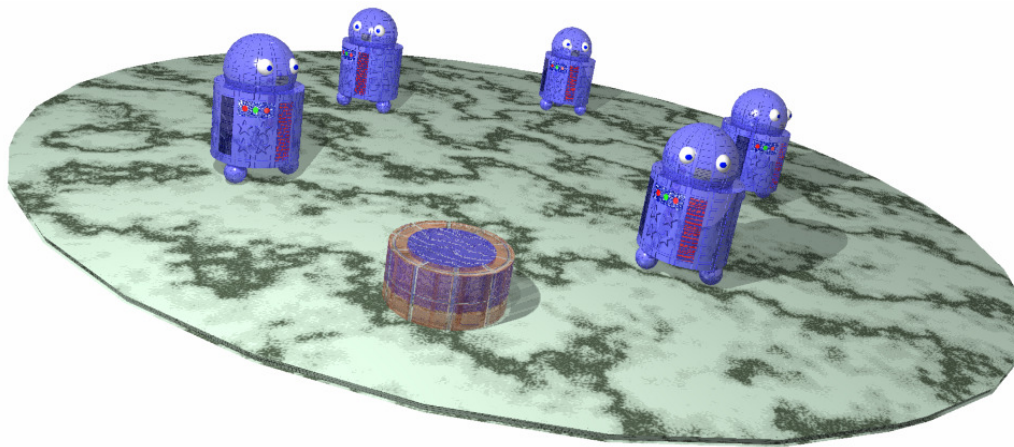
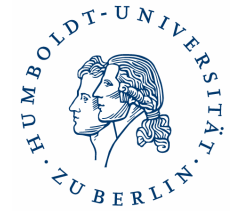
- Dependable architecture for distributed systems
- Alternating consensus/diagnosis phase and execution phase
- No communication during execution phase

# *The Unstoppable Orchestra*

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# Balancing the Robots



- Keeping an instable plate in balance
- A fault may immobilize a robot

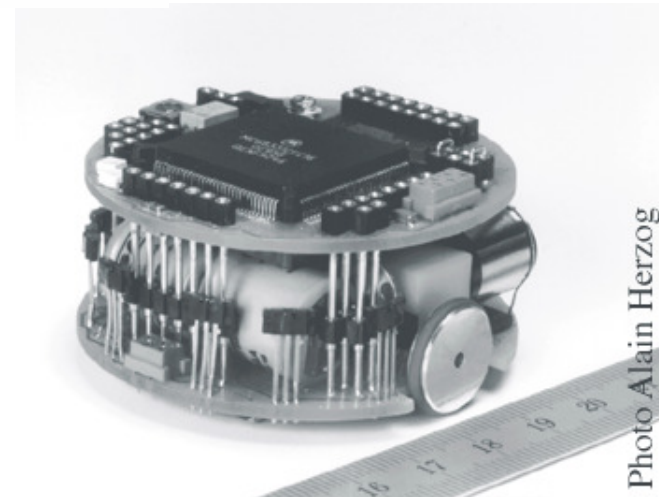
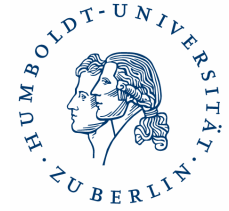


Photo Alain Herzog

# Security by Consensus

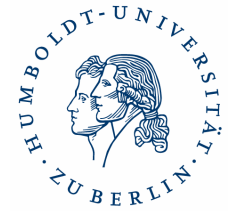


- “Treasure-box” approach, agreement by comparison
- Data are accessible when a weighted majority agrees



# *Implementations*

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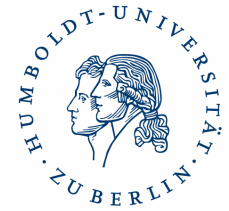


- Multiprocessor diagnosis at JPL (Wang, Blough, Alkalaj, 1994)
- Testing and diagnosis by comparison on the wafer without a golden unit (Rangarajan, Fussell and Malek, 1990, Agrawal, LogiTech)
- Mobile ad-hoc networks (Chessa and Santi, 2001, Elhadef, 2007)
- Data integrity (Ziwich, Duarte and Albini 2005)
- Application-level diagnosis for generic time-triggered systems (Serafini et al 2010, Suri, Kopetz)



# *The System Diagnosis Questions*

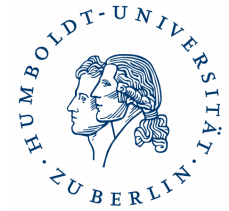
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- Fault models (active nodes only, active and passive nodes, synchronization, frequency)
- Centralized or distributed, hierarchical
- Detection, location, fail-over, recovery
- Coverage, granularity, level, scalability and speed
- Static versus dynamic methods

# *Challenges in the Context of Comparison-based Methods*

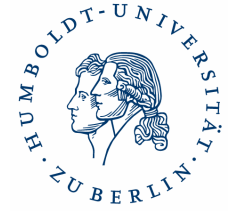
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- What are the most realistic models and assumptions?
- What features/variables should be compared to make diagnosis most effective at each level?
- How to minimize monitoring and comparison overheads, synchronization and frequency?
- Dealing with diversity of HW, SW, people, etc.
- Dealing with uncertainty of comparisons?
- Diagnosis of temporary faults and new problems
- Can exotic faults such as configuration faults be handled by comparison? Encoding configuration
- Keeping it simple

# *Future Applications*

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- Cloud and grid computing
- Multicore and many core systems
- Comparison in new communication environments (especially wireless)
- Data integrity and security
- Embedded systems, sensor networks



## Appendix:

A summary  
of MM and MM\*  
models

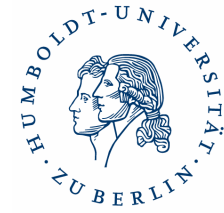
Model	Reference	Main Contributions
MM model	[Maeng and Malek 1981]	<ul style="list-style-type: none"> <li>- comparison diagnosis model in which units are also comparators</li> <li>- comparison outputs when at least one unit is faulty always results in a mismatch</li> <li>- central observer is a trusted unit that performs diagnosis</li> <li>- necessary and sufficient conditions for one-step <math>t</math>-diagnosability</li> <li>- procedure to construct minimal graph for diagnosable systems</li> <li>- evaluation of diagnosis latency in terms of test cycles</li> </ul>
	[Sengupta and Dahbura 1992]	<ul style="list-style-type: none"> <li>- generalization of the MM model: allows comparators to be one of the units being compared</li> <li>- characterization of diagnosable systems under the MM model</li> <li>- diagnosability of general systems is NP-complete</li> </ul>
	[Sengupta and Rhee 1990]	- $t/x$ -diagnosability and $t[x]$ -diagnosability
	[Chen et al. 1993]	- extension of MM model considering processor and comparator faults separately; diagnosability evaluation
	[Wang et al. 1994a; 1994b]	- new necessary and sufficient diagnosability conditions for both the MM model and Sengupta and Dahbura's model
	[Maestrini and Santi 1995]	- correct but incomplete diagnosis algorithm applied to locate faults in bi-dimensional processor arrays
	[Araki and Shibata 2002a]	- diagnosability of $k$ -ary $r$ -dimensional butterfly networks
	[Araki and Shibata 2002b]	- $O(k^2n)$ diagnosis algorithm for butterfly networks
MM* Model	[Maeng and Malek 1981]	- MM* model is a special case of the MM model: each unit compares all pairs of neighbors
	[Sengupta and Dahbura 1992]	<ul style="list-style-type: none"> <li>- diagnosis algorithm with time complexity <math>O(N^5)</math> under the MM* model</li> <li>- diagnosability of general systems under the MM* model is NP-complete</li> </ul>
	[Yang and Tang 2007]	- diagnosis algorithm with time complexity $O(N \times \Delta^3 \times \delta)$ under the MM* model, where $\Delta$ and $\delta$ are respectively the maximum and the minimum degrees of a node
	[Wang 1999]	- diagnosability of hypercubes and enhanced hypercubes
	[Yang 2003]	- worst case $O(N \log_2^2 N)$ diagnosis algorithm for hypercubes
	[Fan 2002]	- diagnosability of crossed cubes
	[Yang et al. 2005]	- $O(N \log_2^2 N)$ diagnosis algorithm for crossed cubes

(from Duarte, Roverli, Ziwich, Albini, 2010)



Model	Reference	Main Contributions
MM* Model (continued)	[Yang and Yang 2007]	- diagnosability of locally twisted cubes - $O(N \log_2^2 N)$ diagnosis algorithm for locally twisted cubes
	[Chiang and Tan 2007]	- diagnosability of hypercube-like networks
	[Zheng et al. 2002]	- diagnosability of star graphs
	[Lai et al. 2004]	- diagnosability of matching composition networks
	[Chang et al. 2007]	- $(t, k)$ -diagnosis for matching composition networks
	[Chang et al. 2004]	- diagnosability of $t$ -connected networks - diagnosability of product networks
	[Sheu et al. 2008]	- strong diagnosability of $t$ -regular and $t$ -connected networks
	[Hsieh and Chen 2008a]	- strong diagnosability of product networks: hypercubes, mesh-connected $k$ -ary $n$ -cubes, torus-connected $k$ -ary $n$ -cubes, hyper-Petersen networks
	[Hsieh and Chen 2008b]	- strong diagnosability of matching composition networks: $n$ -dimensional crossed cubes, Möbius cubes, twisted cubes and locally twisted cubes
	[Chessa and Santi 2001]	- comparison-based diagnosis applied for mobile ad hoc networks - Static-DSDP protocol for fixed topology
	[Elhadef et al. 2006b]	- protocol Dynamic-DSDP for ad hoc networks based on Chessa and Santi's model
	[Elhadef et al. 2006a; 2007]	- comparison-based diagnosis applied for mobile ad hoc networks - Adaptive-DSDP Protocol for fixed topology networks - Mobile-DSDP protocol for time-varying topology networks
[Chiang and Tan 2009]	- node diagnosability based on extended star structures	
Broadcast Comparison Model	[Blough and Brown 1999]	- fully distributed comparison model - based on MM* for systems with reliable broadcast - polynomial-time algorithms to diagnose static and dynamic fault situations
Generalized Distributed models	[Albini et al. 2005; Albini and Duarte Jr. 2001]	- the generalized distributed comparison-based model: a hierarchical, adaptive and distributed model based on Sengupta and Dahbura's model - <i>Hi-Comp</i> diagnosis algorithm: requires at most $O(N^3)$ comparisons and has worst-case latency of $O(\log_2 N)$ rounds
	[Ziwich et al. 2005]	- generalized distributed comparison-based model assuming the comparison of faulty units outputs may match - <i>Hi-Dif</i> diagnosis algorithm that requires at most $O(N^2)$ comparisons and has worst-case latency of $O(\log_2 N)$ latency

(from Duarte, Roverli, Ziwich, Albini, 2010, continued)



Model	Reference	Main Contributions
Probabilistic model	[Dahbura et al. 1987]	- probabilistic comparison based model - considers probabilities for a match or a mismatch when comparing units
	[Rangarajan and Fussell 1988]	- strategy based on the evaluation of multiple syndromes
	[Fussell and Rangarajan 1989]	- $O(\log_2 N)$ for the evaluation of multiple syndromes
	[Lee and Shin 1994]	- probably optimal algorithm for the evaluation of multiple syndromes
	[Choi and Jung 1990]	- diagnosis algorithm for sparsely interconnected systems
$(p, k)$ -Probabilistic model	[Pelc 1991]	- a task has $k$ possible outcomes - each unit has the same probability $p < 1/2$ - probability of obtaining a match when comparing a faulty unit and a fault-free unit or two faulty units is $q = 1/k$ - <i>diagnosis</i> and the <i>diagnosability</i> problems are NP-hard for general topology
	[Blough and Pelc 1992]	- polynomial time diagnosis algorithms for bipartite graphs (includes hypercubes, grids and forests) - linear-time algorithm to perform optimal diagnosis of rings
Evolutionary Comparison-Based models	[Elhadef and Ayeb 2001a]	- evolutionary comparison-based diagnosis
	[Abrougui and Elhadef 2005]	- parallel evolutionary diagnosis models
	[Elhadef et al. 2006]	- comparison-based diagnosis model with an artificial-immune-system-based approach

(from Duarte, Roverli, Ziwich, Albini, 2010 , continued)