

# **A Look at Dependability and Synchrony in Distributed Mobile Robotic Systems:**

## **Adding Some Pragmatism to Theory**

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# Context / Motivation

- **Context**

- Given: Multiple robots
- Obtain: Single system

- **Requirements**

- Deterministic solutions
- Use little / no infrastructure
- Weak / weaker / weakest assumptions

- **Characteristic**

- Start from theory, move toward practice

# Outline

- **Part I: Gathering problem**
  - Limited visibility
  - No communication
  - Compasses
- **Part II: Collision avoidance**
  - No visibility
  - Limited communication
- **Conclusion**

# PART I

**with:**

- Samia Souissi (JAIST)
- Masafumi Yamashita (Kyushu Univ.)

# Motivation

- **Context**

- Autonomous robots
- No infrastructure
- No common knowledge (e.g., coordinate system)

- **Question**

- What are the

**fundamental limits to robust coordination?**

# Gathering Problem

- **Gathering**
  - Set of robots located arbitrarily
    - ➔ All robots gathered at same location
- **Provides**
  - Agreement on common origin
- **Desired property**
  - Self-stabilization

# System Model

- **Environment**

- Euclidean plane
- No landmarks
- No obstacles
- No boundaries

- **Robots**

- Location: single point
- Collocation possible; “no collisions”
- Own coordinate system:  
origin, directions, unit distance

# System Model

- **Interactions**

- **Vision:** get position of robots
- No explicit communication
- No global coordinates

- **Activations**

- Cycle: *Look - Compute - Move - ...Sleep...*
- Deterministic algorithm
- **Oblivious** (stateless)  
=> self-stabilizing



# System Model

- **Two Variants**

- **Semi-Synchronous**

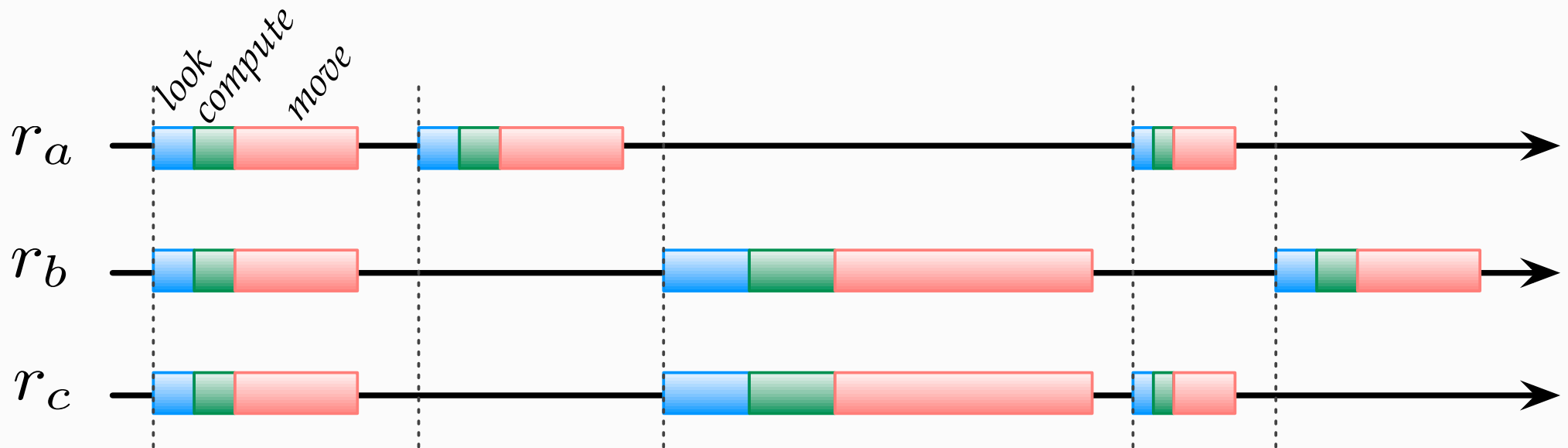
[SY99] Suzuki, Yamashita. Distributed Anonymous Mobile Robots. *SIAM J. Comput.*, 28(4):1347–1363, 1999.

- **Asynchronous**

[FPSW05] Flocchini, Prencipe, Santoro, Widmayer. Gathering of asynchronous robots with limited visibility. *Theor. Comp. Sci.*, 337:147–168, 2005.

# Semi-Synchronous

[SY99] Suzuki, Yamashita. Distributed Anonymous Mobile Robots. *SIAM J. Comput.*, 28(4): 1347–1363, 1999.

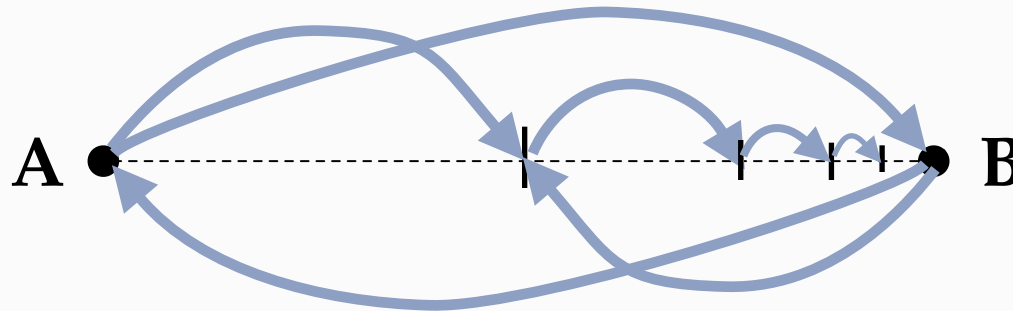


## ● Activation Schedule

- Atomic cycle: (*Look - Compute - Move*)
- Parallel: see same thing
- Sequential: one see preceding movement

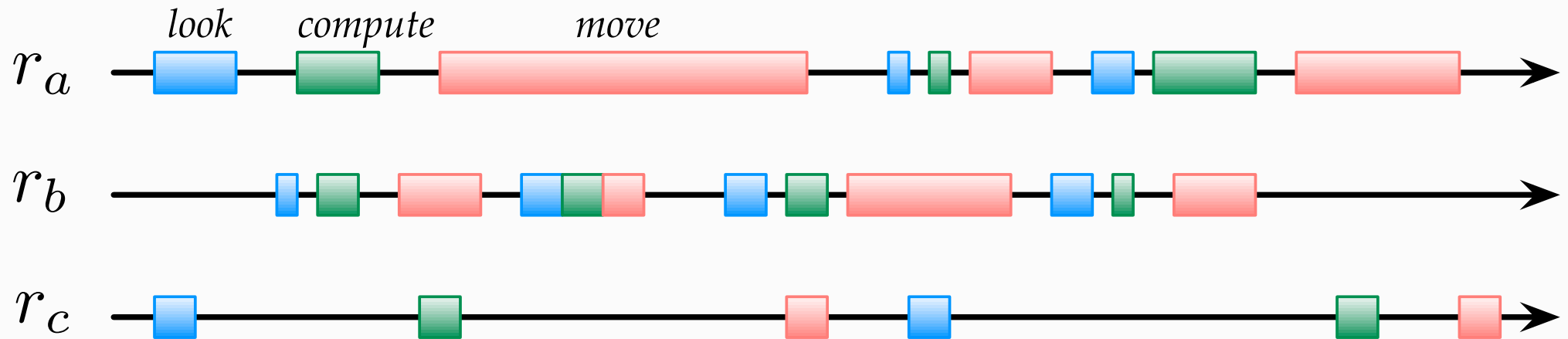
# Gathering Problem

- **Goal**
  - From any configuration,
  - Eventually, all robots gather at single location
- **Difficulty: simple illustration**
  - Two robots A, B in semi-synchronous model



# Asynchronous

[FPSW05] Flocchini, Prencipe, Santoro, Widmayer. Gathering of asynchronous robots with limited visibility. *Theor. Comp. Sci.*, 337:147–168, 2005.



- **No synchronization**
  - Can be seen while moving
  - Cannot anticipate others' moves

# Convergence vs. Formation

- **Convergence**

- Solve problem **asymptotically**
- Trivial to achieve (e.g., barycenter)

- **Formation**

- Solve problem **deterministically**
- Difficult to achieve
- Need to break symmetry

# Gathering w/Limited Visibility

- **Assumption**

- Visibility graph connected initially

- **Safety**

- Keep visibility graph connected

- **Why?**

- Partition unrecoverable
  - Oblivious robots
  - => forget about each other's existence
  - => gathering at more than one point (invalid)

# Gathering Possible

- **...in Semi-synchronous model**

- proved in [SY99]
- **Non-oblivious** robots
- **Full** visibility

- **...in Asynchronous model**

- proved in [FPSW05]
- **Oblivious** robots
- **Limited** visibility
- **with compass** (i.e., shared orientation)

# Gathering w/Compass

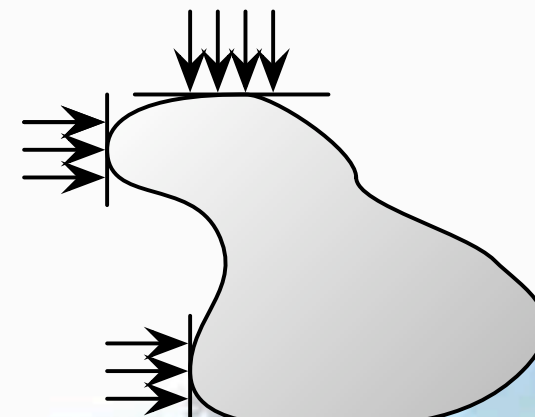
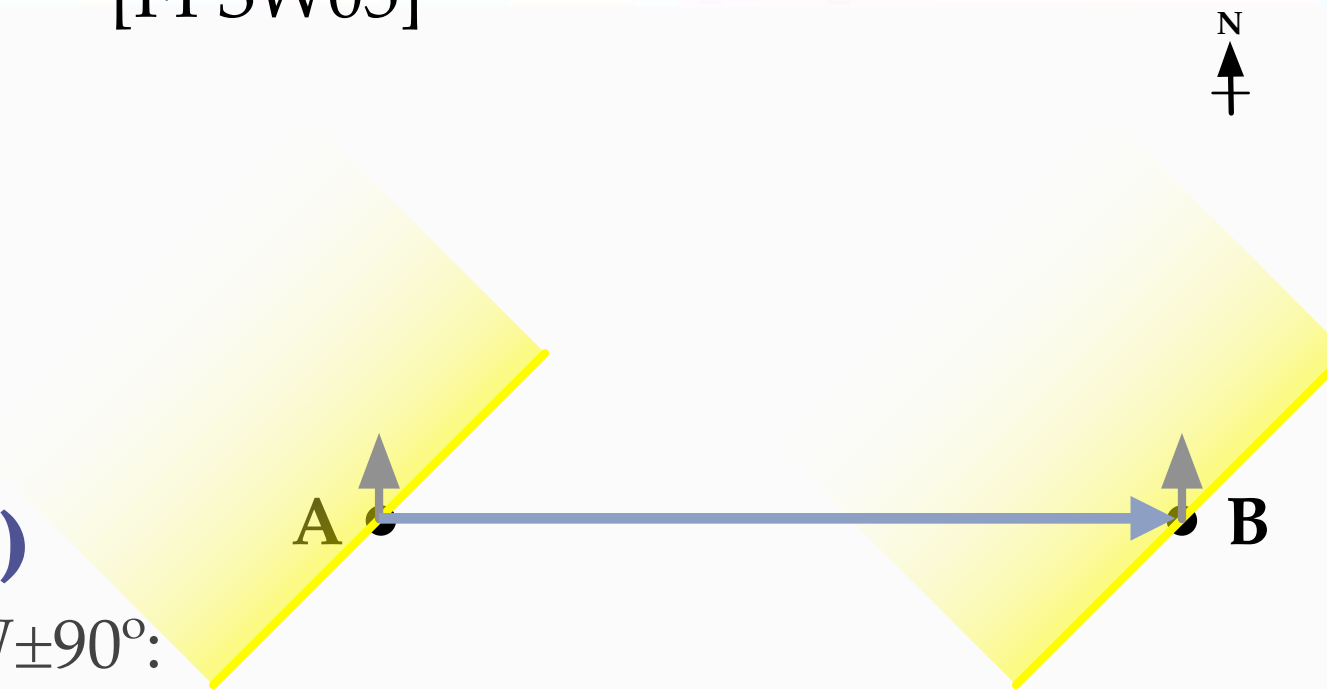
[FPSW05]

- **Role**

- Break symmetry

- **Idea (2 robots)**

- Other robot to  $NW \pm 90^\circ$ :
  - Wait
- Otherwise
  - Move to other robot





# Question

[SDY06]

- **What if**  
compasses are **unreliable?**
- **Especially**
  - Transient failures
  - Interference
  - Stabilization

# Unreliable Compasses

- **Compass**

- Function of (time, robot)  $\rightarrow$  direction

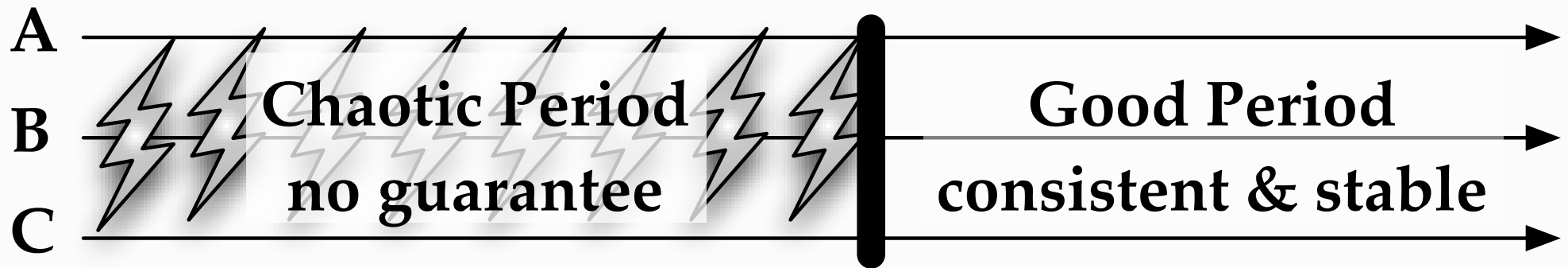
- **Perfect compasses**

- Consistency: all compasses point to the same direction
- Stability: compasses never change

- **Eventually-consistent Compasses**

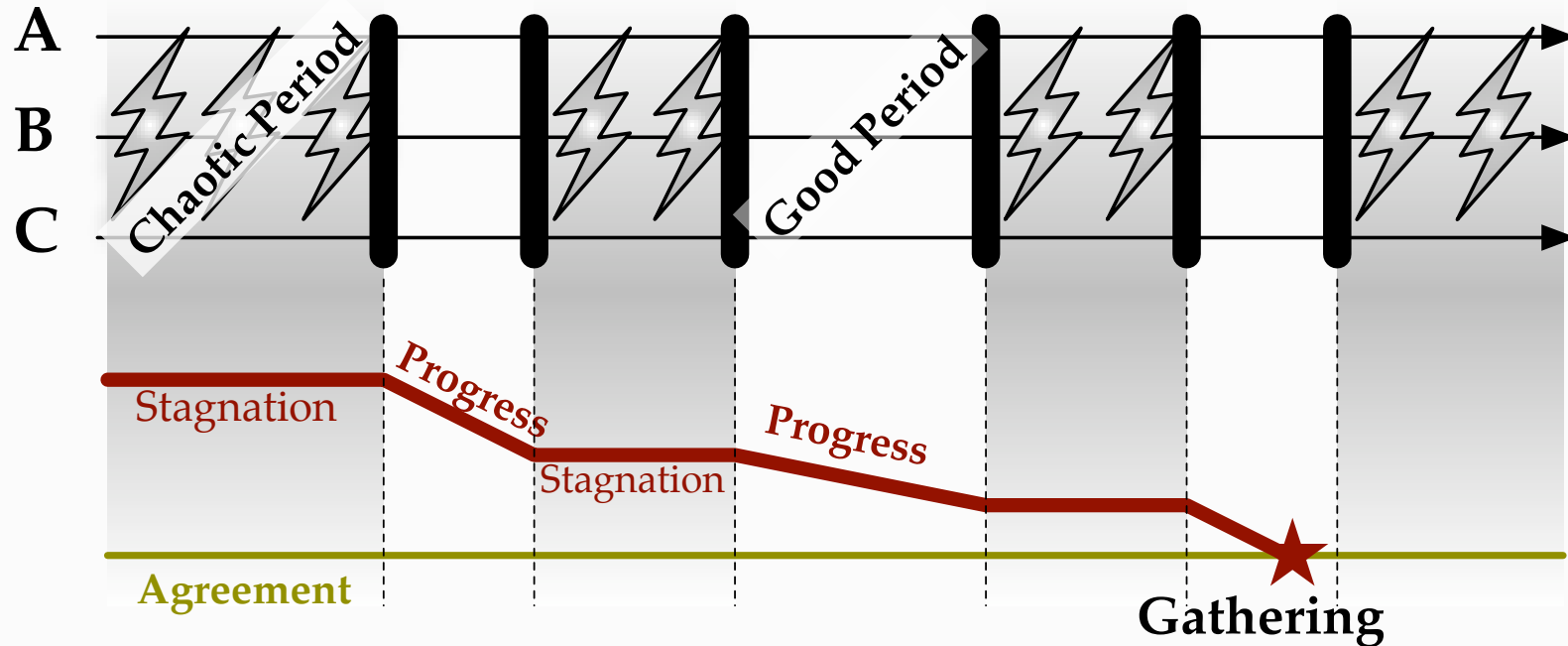
- There is a time (unknown) after which compasses are:  
**consistent & stable**

# Unreliable Compasses



- **Chaotic period**
  - Safety: OK; Progress: *maybe*
- **Good period**
  - Safety: OK; Progress: OK

# Unreliable Compasses



- **Practically speaking...**

- Need good periods “long & frequent enough”
- Algorithm tolerates unbounded number of transient failures

# Gathering w/Unreliable Comp.

		Perfect Compass	Eventual Compasses	No Compass
<b>Asynch. Model</b>	$n \geq 4$	[FPSW05]	Impossible	Impossible
	$n=2,3$			
<b>Semi-synchronous Model</b>	$n \geq 3$	([SDY06])	[SDY06]	[SY99]
	$n = 2$			Impossible

# Gathering w/Unreliable Comp.

- **Algorithm**

- Use perfect compasses  
or
- Use semi-synchrony

- **Impossible case**

- Asynchronous,  $n \geq 4$ 
  - Algorithm [SDY06]  $\Rightarrow$  breaks visibility
  - Best possible: Admits deadlock situations

# Some Future Work

- **Unreliable compasses**
  - with bounded imprecisions
- **Faulty robots**
  - Byzantine robots
- **Dynamic problems**
  - Flocking, etc...

# PART II

**with:**

- Julien Cartigny (Univ. Limoges, France)
- Nak Young Chong (JAIST)
- Rami Yared (JAIST)
- Matthias Wiesmann (JAIST)



# Motivating Context

- **Equipment**

- 4 Pioneer-3 robots
  - Laptop
  - Wireless (WiFi; bluetooth)
  - Sonar (180°, 6-7m)

- **Objective**

- Group movement without collisions

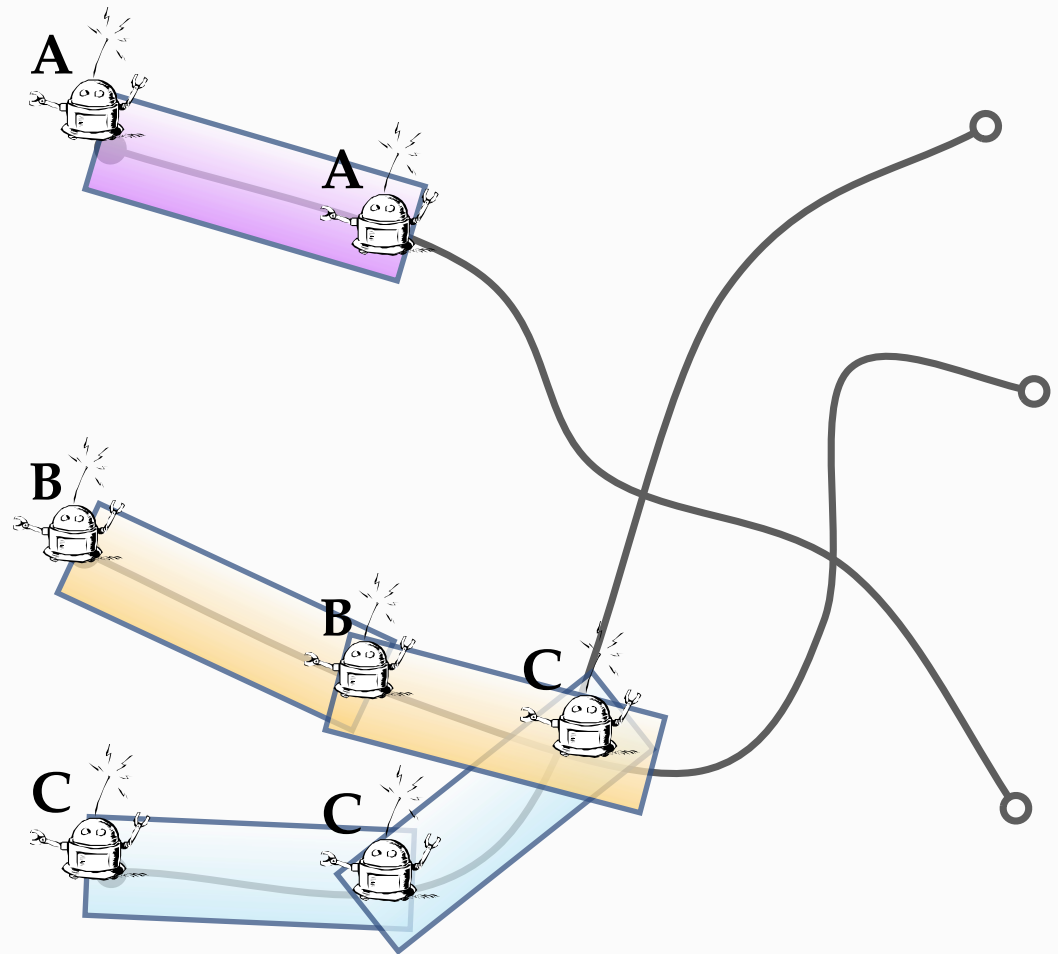
- **Desired Properties**

- Decentralized solution
- Fault-tolerance
- Fail-safe behavior



# Path Reservation

- **Robot knows**
  - own destination / path
  - own location
  - information in messages
- **Does NOT know**
  - others' destinations
  - others' location
  - others' velocity
  - communication delays



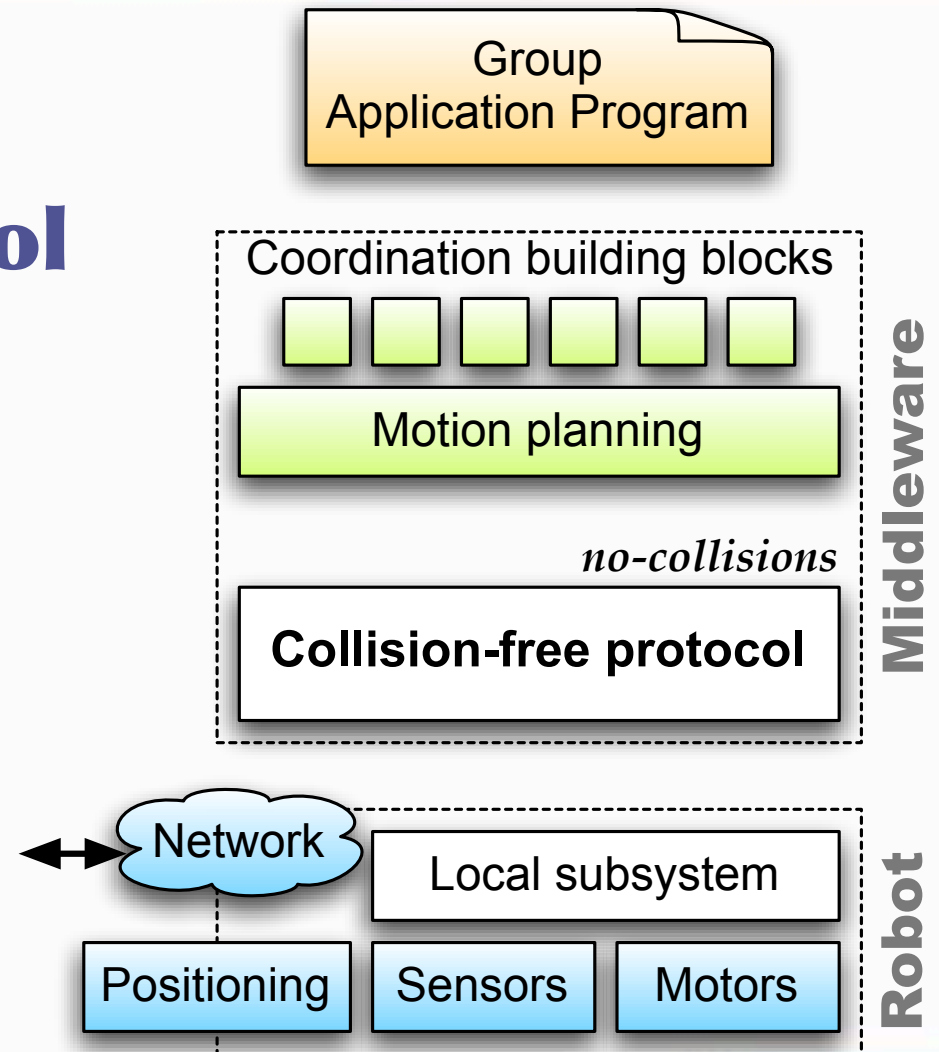
# Architecture

- **Collision-free protocol**

- Ensure no-collision
- Fail-safe behavior

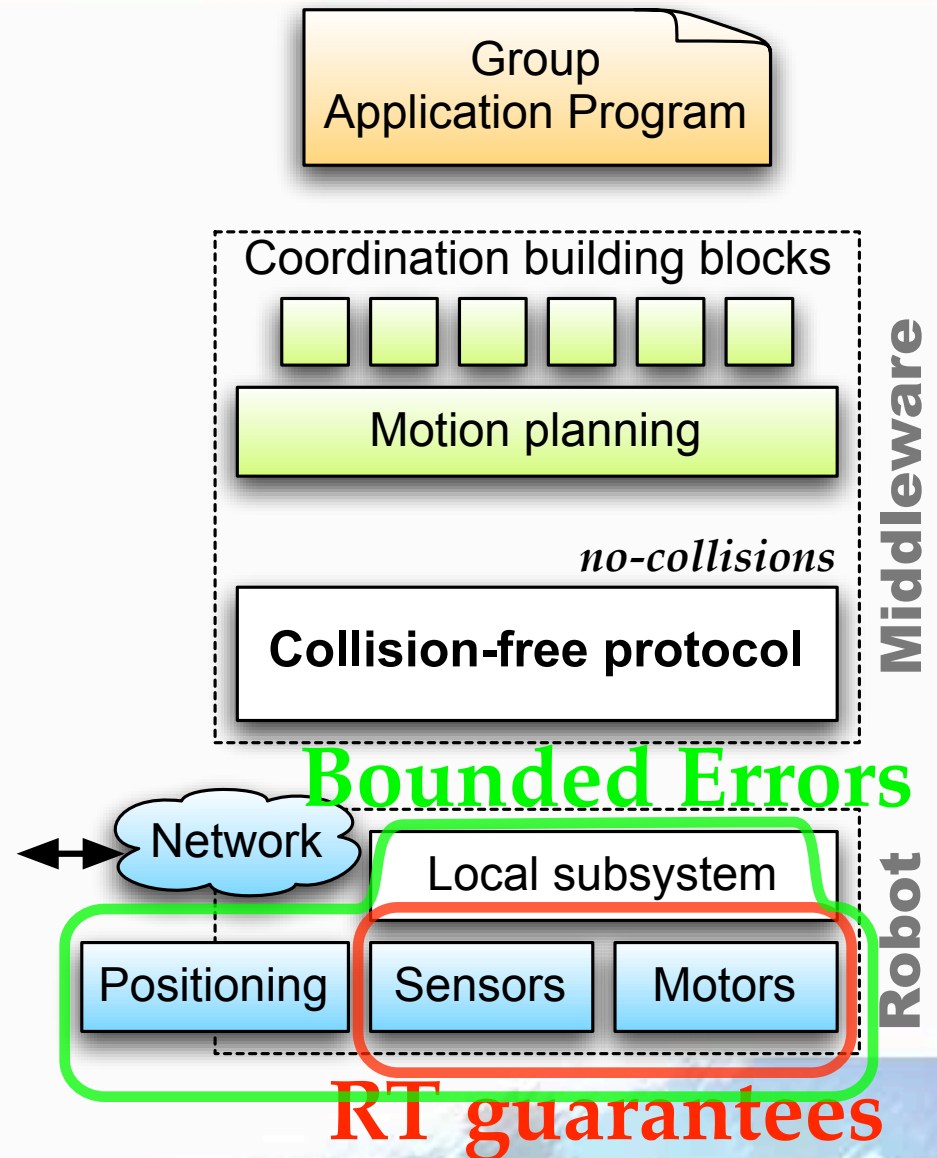
- **Local subsystem**

- Individ. robot movements
- Detect inert obstacles
- Use sonars



# Assumptions

- **Real-time**
  - Local subsystem
  - Sensors (sonars)
  - Motor control code



# System Model

- **Robots**
  - Have footprint
  - No vision
  - Ad hoc wireless communication
- **Positioning System**
  - Global  $x$ - $y$  referential
  - Robot can query asynchronously
  - Robots get **own position**
- **Communication**
  - Time-free
  - Two models: full, ad hoc

# Path Reservation

- **Idea**

- Similar to database locking

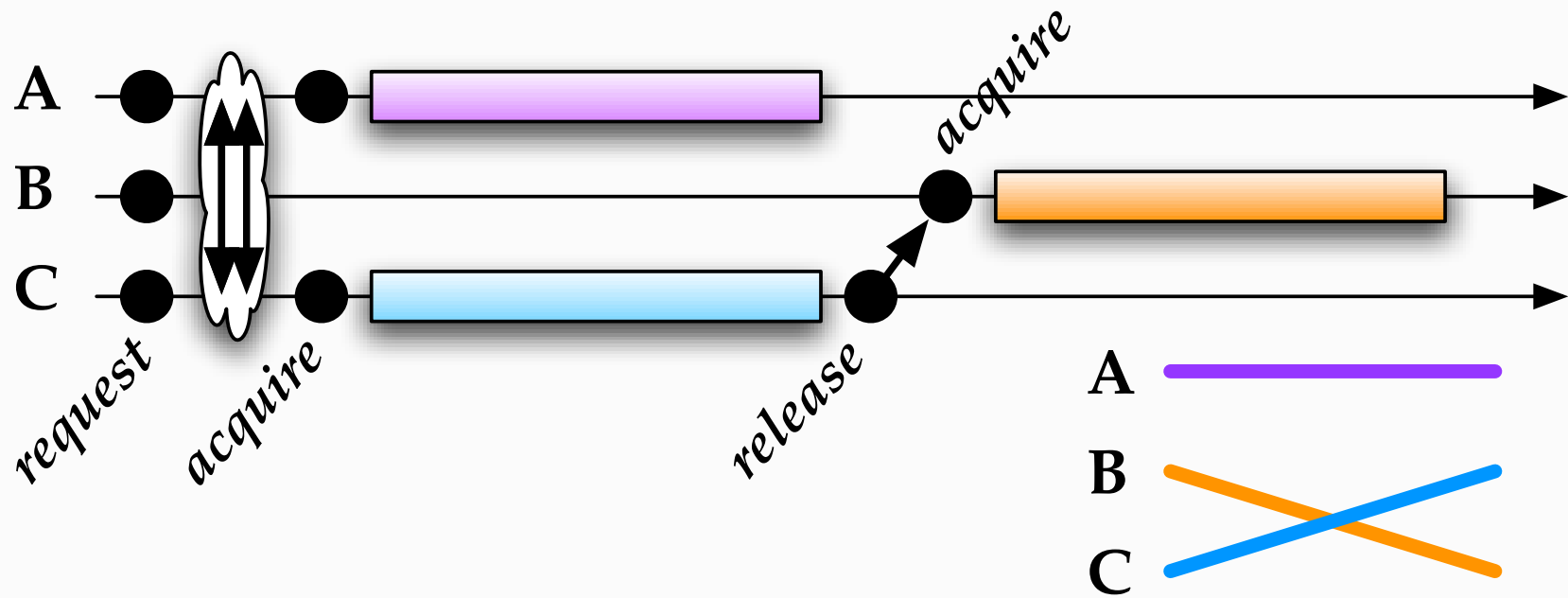
- **Primitives**

- *acquire*: request lock on a zone
- *release*: release zone

- **Benefits**

- Prevent collisions
- Provides some information on location

# Path Reservation



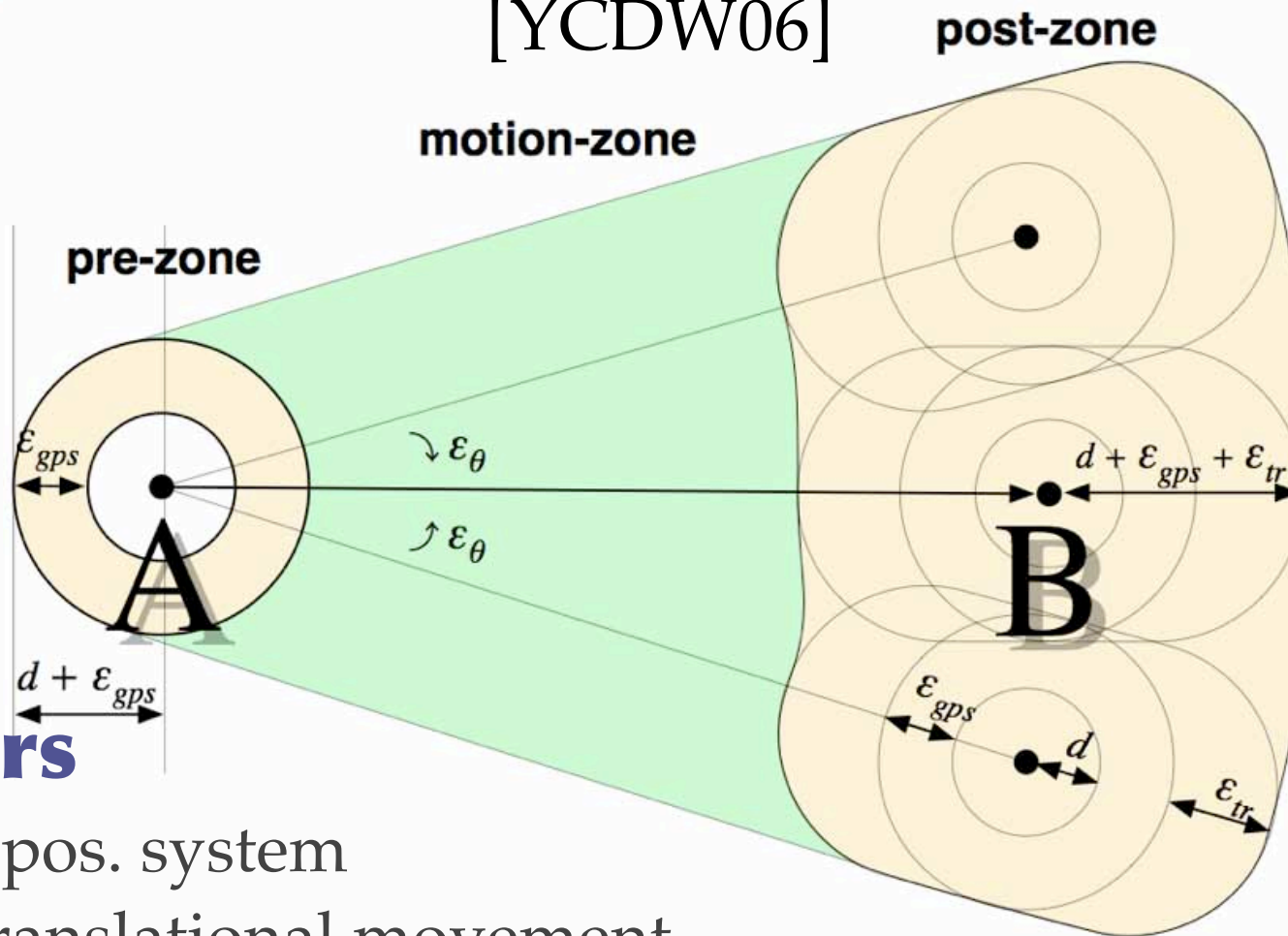
- **Desired properties**

- Mutual exclusion between conflicting requests
- No starvation of requests (unless deadlock)



# Anatomy of a Zone (errors)

[YCDW06]



## ● Errors

- $\epsilon_{gps}$  : pos. system
- $\epsilon_{tr}$  : translational movement
- $\epsilon_{\theta}$  : rotational movement (incl. sensors)



# Model 1: Fully connected

- **Model**

- All robots “know” each other
- All robots can communicate
- Communication is reliable asynchronous

- **Purpose**

- Few robots
- Limited area

- **Benefit**

- Simple, fault-tolerant solution

# Model 1: Reservation

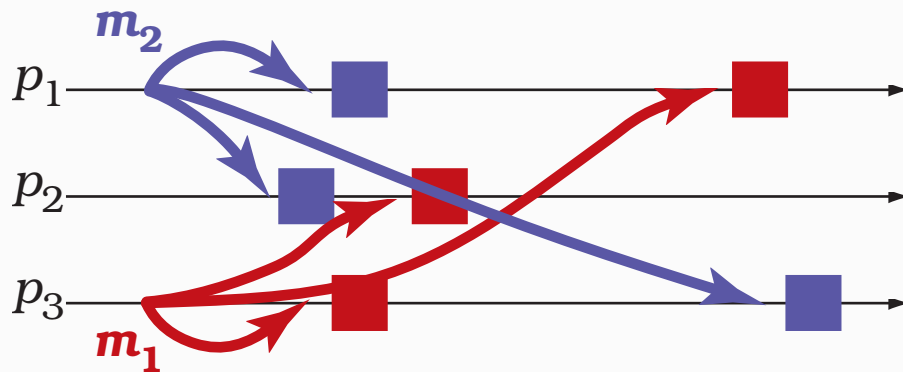
- **Idea**

- Use Total Order Broadcast protocol

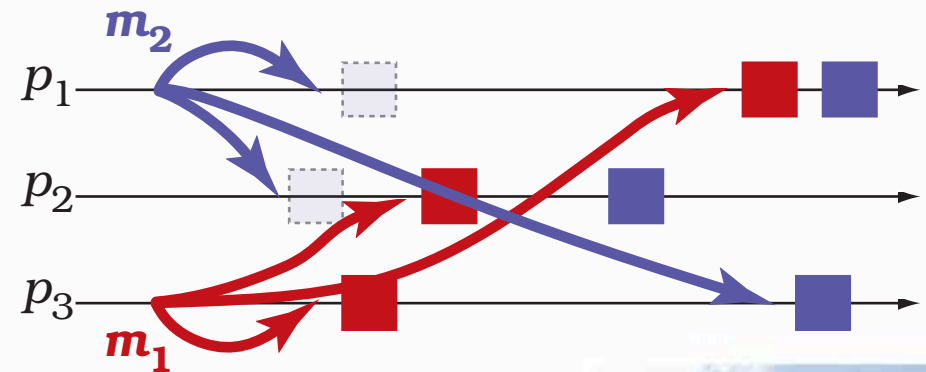
## Total Order Broadcast

- Broadcast primitive
- Hosts deliver same sequence of messages

### Ordinary Broadcast



### Atomic Broadcast



# Model 1: Reservation

- **Idea**

- Use of Total Order Broadcast

- **Advantages**

- Well-known requirements
- Many algorithms (see survey [DSU04])
- Fault-tolerant solutions  
(e.g., with unreliable FDs & maj. correct hosts)

- **Synchrony assumption**

- E.g., unreliable failure detectors
- FAIL => liveness violation

# Model 1: Protocol

- **To move**

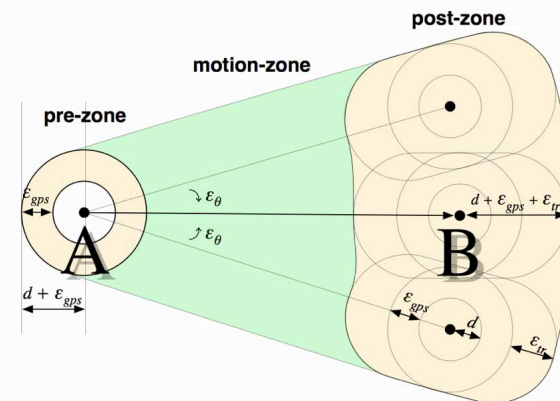
- Get own position
- Compute zone  $Z$
- TO-bcast(*Request*,  $Z$ )

- **When TO-deliver (*Request*,  $Z$ )**

- If conflict  $\Rightarrow$  put  $Z$  in pending requests
- Else lock( $Z$ )

- **When lock( $Z$ )**

- Move along  $Z$
- Wait until destination reached
- Get own position; compute new pre-zone
- R-bcast(*Release*,  $Z$  - new pre-zone)



# Model 1: Drawbacks

- **Limited scalability**
  - Protocol involves all robots
  - ... regardless of actual location
- **Limited flexibility**
  - Requires initial knowledge of all robots
- **Energy consumption**
  - Requires coverage of whole area  
(or supplemented by routing)

# Model 2: Ad hoc

[YCDW06]

- **Limited communication range**
  - Known to all robots:  $D$   
(NB:  $D$  can be minimum of all ranges)
- **Asynchronous**
  - No bounds on message delays  
(e.g, because of retransmission).
- **Neighborhood discovery primitive**
  - Get set of **direct** neighbors
  - **Query** based primitive
  - **Stronger** guarantees

# Model 2: Neighborhood Discovery

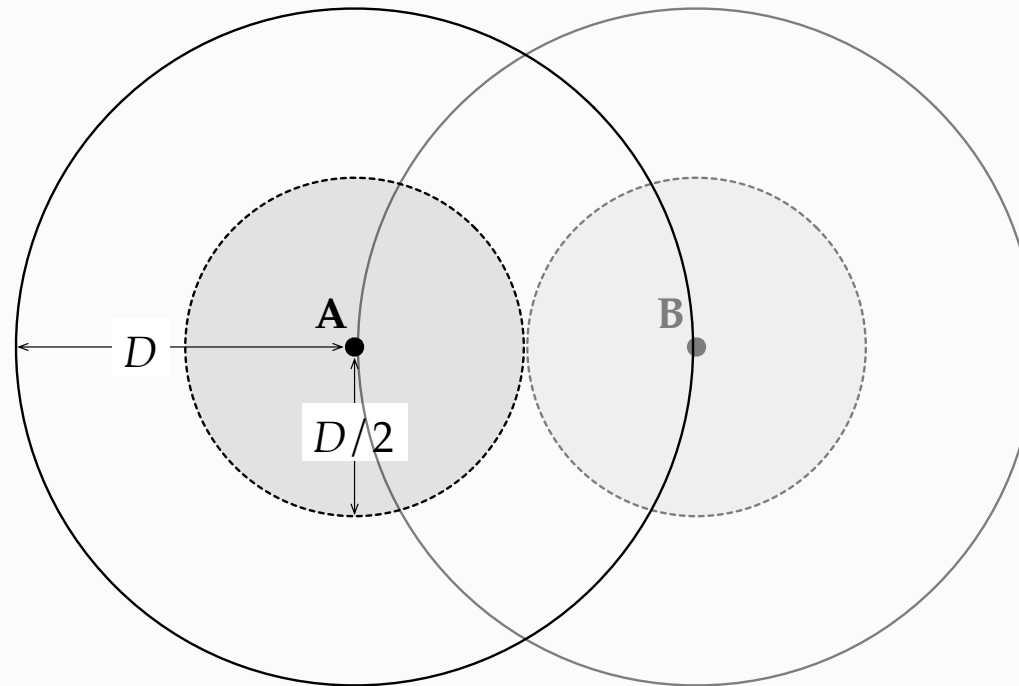
- **Primitive**

- Query by robot  $R$  at time  $t$
- Return set  $Neighbors(r,t)$

- **Query period**

- From *query* to *return*
- For each robot  $s'$ ; during query period:
  - $s'$  in range  $\Rightarrow s'$  in  $Neighbors(r)$
  - $s'$  not in range  $\Rightarrow s'$  not in  $Neighbors(r)$
  - $s'$  partially in range  $\Rightarrow$  undetermined.

# Model 2: Restrictions



- **Restriction**

- Reservations within  $D/2$  (- errors)

- **Ensures**

- Cannot conflict without being “introduced”



# Model 2: Discussion

- **Advantage**
  - Dynamic groups
  - Locality-preserving
  - Scalable
- **Drawback**
  - No fault-tolerant protocol yet
- **Synchrony assumption**
  - Neighborhood discovery
  - FAIL => safety violation

# Future Directions

- **Protocol extension**
  - pipelining / interleaving
- **Parameter dimensioning**
  - robots density
  - robot speed / acceleration / braking distance
  - communication range
  - communication delays
  - errors

# Conclusion

- **Part I**

- Study limits of coordination
- Tolerate faulty compasses

- **Part II**

- Use communication & location
- Reservation system
- Full connected: simple, FT
- Ad hoc: scalable, flexible

- **Theory: still a long way to go...**

# References

## ● Models

- [SY99] Suzuki, Yamashita. Distributed Anonymous Mobile Robots. *SIAM J. Comput.*, 28(4):1347–1363, 1999.
- [FPSW05] Flocchini, Prencipe, Santoro, Widmayer. Gathering of asynchronous robots with limited visibility. *Theor. Comp. Sci.*, 337:147–168, 2005.

## ● Gathering

- [AP04] Agmon, Peleg. Fault-tolerant gathering algorithms for autonomous mobile robots. *SODA 2004*. LNCS.
- [CP02] Cieliebak, Prencipe. Gathering autonomous mobile robots. *SIROCCO 2002*. LNCS.
- [Pre05] Prencipe. The effect of synchronicity on the behavior of autonomous mobile robots. *Theory Comput. Syst.* 38(5): 539-558, 2005.

## ● **Unreliable compasses**

- [SDY05] Souissi, Défago, Yamashita. Eventually consistent compasses for robust gathering of asynchronous mobile robots with limited visibility. JAIST, IS-RR-2005-010, July 2005.

## ● **Other formation problems**

- [DK02] Défago, Konagaya. Circle formation for oblivious anonymous mobile robots with no common sense of orientation. *POMC 2002*.
- [GP04] Gervasi, Prencipe. Coordination without communication: the case of the flocking problem. *Discr. Applied Math.* 144(3): 324-344, 2004.

## ● Collisions

- [VCC+02] Veríssimo, Cahill, Casimiro, Cheverst, Friday, Kaiser. CORTEX: towards supporting autonomous and cooperating sentient entities. *Proc. European Wireless*, 2002.
- [NS03] Nett, Schemmer. Reliable real-time communication in cooperative mobile applications. *IEEE Trans. Computers*, 52(2): 166-180 (2003)

## ● Path reservation

- [YCDW06] Yared, Cartigny, Défago, Wiesmann. Locality-preserving distributed path reservation protocol for asynchronous cooperative mobile robots. JAIST, IS-RR-2006-003, Feb. 2006.